

Principles of Unsaturated Soil Mechanics and Its Application in Geotechnical and Pavement Engineering

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NRRA Webinar May 19, 2020









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- Due to large participation, please type any question or comment on chat box. Moderator will ask questions to Panelists during QA sessions
- Webinar organizers are not planning to provide a certificate of participation. However, to best of our knowledge, this course/activity meets continuing education requirements for PDHs as outlined in Minnesota Statute 326.107. (Please check your state statute)



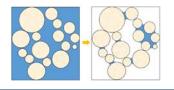






#### Agenda

- Welcome Introduction *T. Beaudry*
- Fundamental Concepts in Unsaturated Soil W. Likos
- Measurement of Unsaturated Properties *R. Velasquez*
- Q&A Fundamentals All
- <u>Break (10 min)</u>
- Impact of Moisture on Pavement Foundation Materials B. Cetin
- Importance of Unsaturated Soil Mechanics in ME Design *B. Cetin*
- Correlations between Unsat Soil Parameters and ME Design Input B. Cetin
- Use of Unsaturated Soil Mechanics by MnDOT-J. Siekmeier
- Q&A Applications All
- Closing Remarks *T. Beaudry*



#### Introduction

#### Terry Beaudry P.E.

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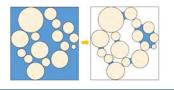






## Why Should I Care?

- Recent developments in soil mechanics warrant a change in classic conservative approach
- Saturated conditions is not appropriate design assumption in explaining heave of road foundations, through swelling of expansive subgrades soils
- Technology has improved our ability to measure and characterize unsaturated soil
- Designing based upon saturated conditions is too conservative and more costly



#### Principles of Unsaturated Soil Mechanics

William J. Likos, PhD Gary Wendt Professor and Department Chair University of Wisconsin-Madison <u>likos@wisc.edu</u>

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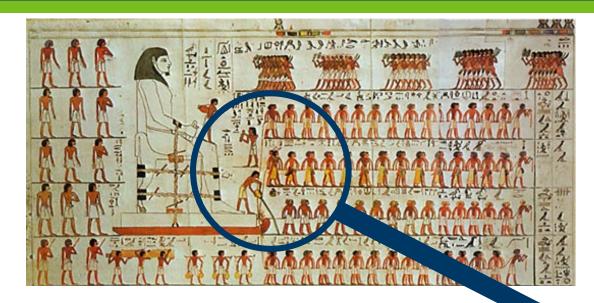
Department of Civil and Environmental Engineering UNIVERSITY OF WISCONSIN-MADISON



# Unsaturated Soil Mechanics and the Great Pyramids?



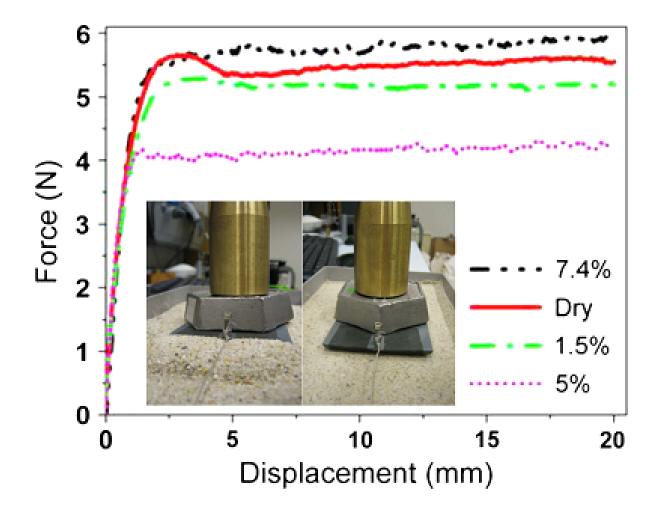
## Wall painting from 1880 B.C. on the tomb of Djehutihotep in southeastern Egypt (Newberry, 1895).



Colossal statue of Djehutihotep (7 m high) transported by 172 workers using ropes and a slide.

Water being poured in the path of the sled.

**Ritual or Unsaturated Soil Mechanics?** 



(from Fall et al., 2014, Phys. Rev. Letters, 112, 175502)

## **Topics for Discussion**

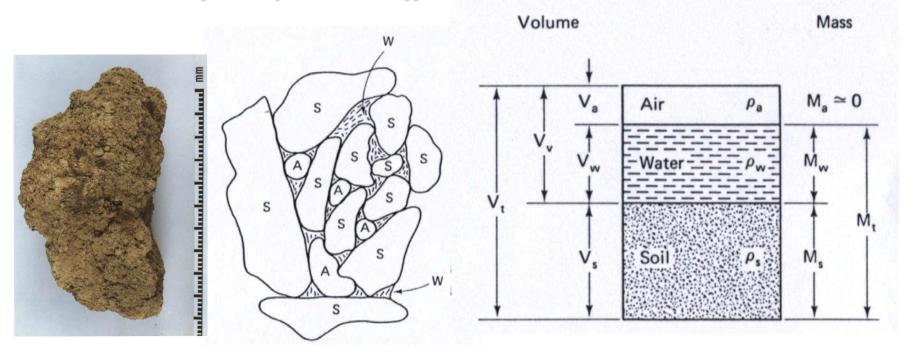
- What is unsaturated soil?
  - Soil as a multiphase system
  - Properties depend on degree saturation
- What are differences between saturated and unsat. soils?
  - Concepts from interfacial physics
- What is soil suction?
  - Concept of pore water potential
- Why is unsaturated soil mechanics important?
  - Examples of engineering problems with unsat. soils.

#### Soil is a multiphase system

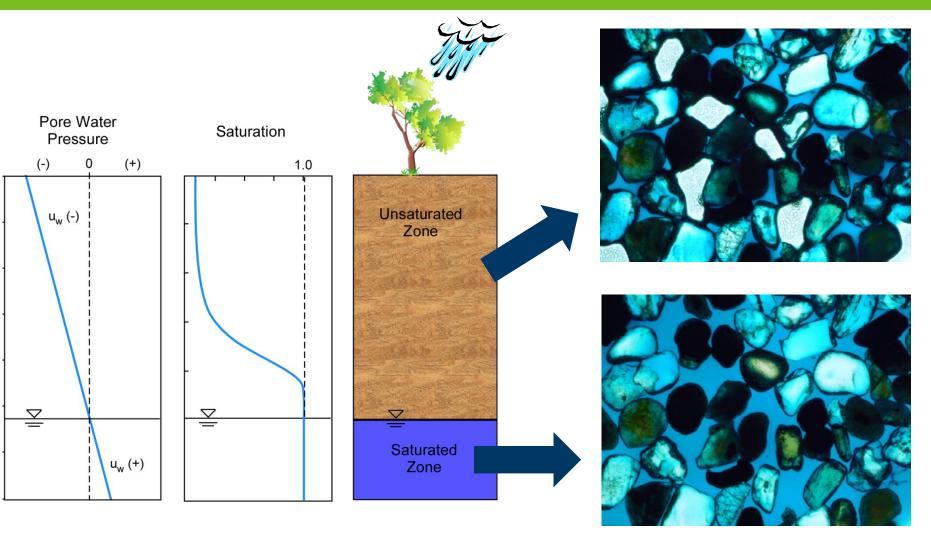
W = Water

A = Air

#### Relative amount of each phase will affect behavior



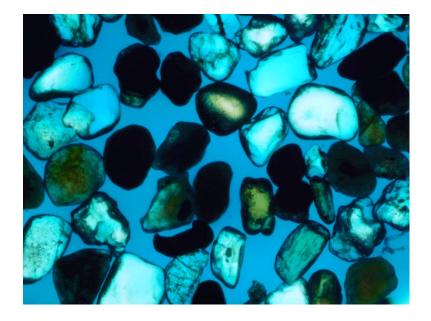
"block diagram"



Aeolian Sand – Alamosa, CO Average Grain Diameter =  $150 \ \mu m$ .

#### Saturated Soil

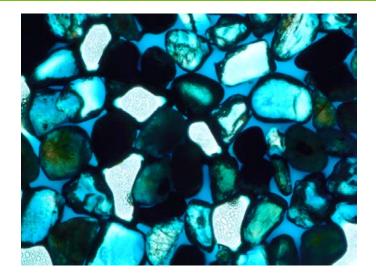
- 2-Phase System
- Pore Fluid Pressure,  $u_w$  $u_w(+)$
- •Volumetric Water Content,  $\theta$  $\theta = V_w/V_t = V_v/V_t = n$
- Degree of Saturation, S  $S = V_w/V_v = 1.0 (100\%)$



• Conductivity (hydraulic, thermal) is constant at constant state (volume, temp.)

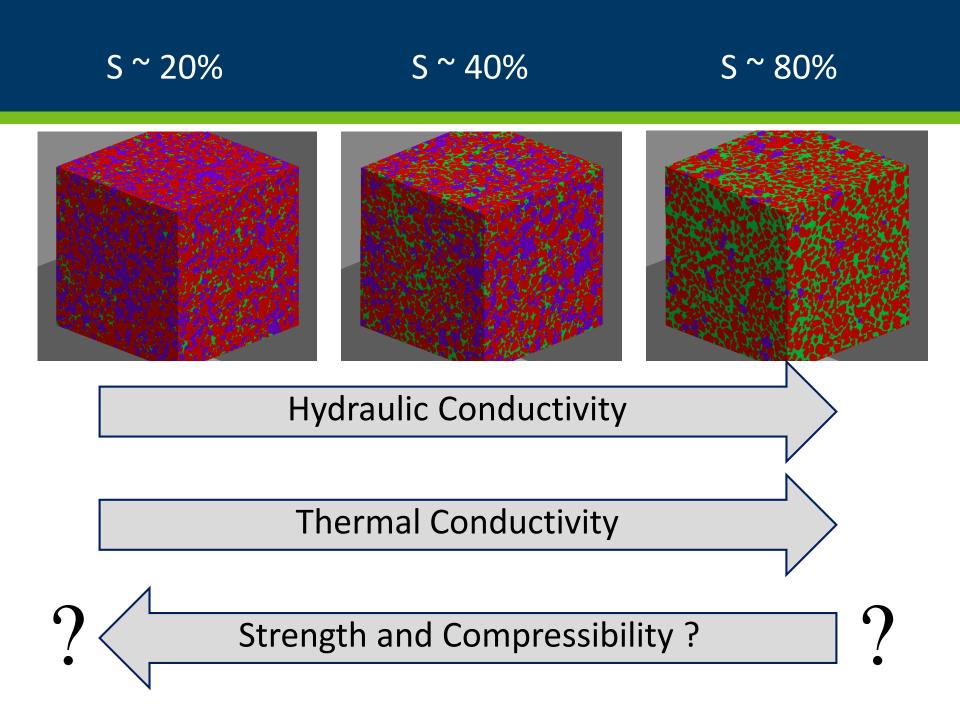
#### **Unsaturated Soil**

- 3-Phase System
- Pore Fluid Pressure,  $u_w$  and  $u_a$   $u_a = 0$  (atmospheric)  $u_w < u_a$  $\psi = u_a - u_w$  (matric suction)
- •Volumetric Water Content,  $\theta$  $\theta = f(\psi), \ 0 < \theta < n$
- Degree of Saturation, S
   S = f(ψ), 0 < S < 1.0</li>
- Hydraulic Conductivity, k  $k = f(\theta)$ or  $k = f(\psi)$



*Soil-water characteristic curve (SWCC)* 

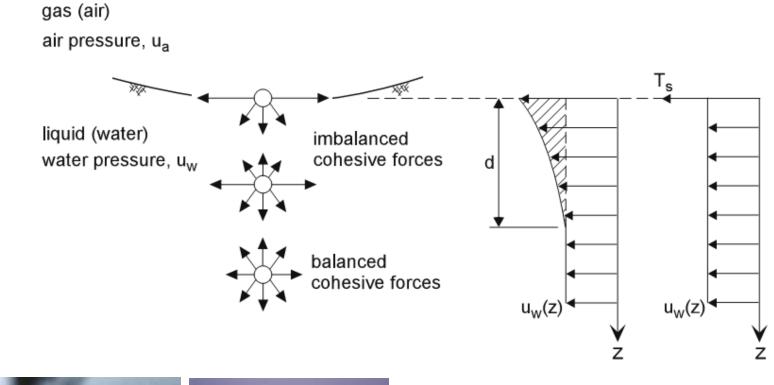
Hydraulic conductivity function (HCF)



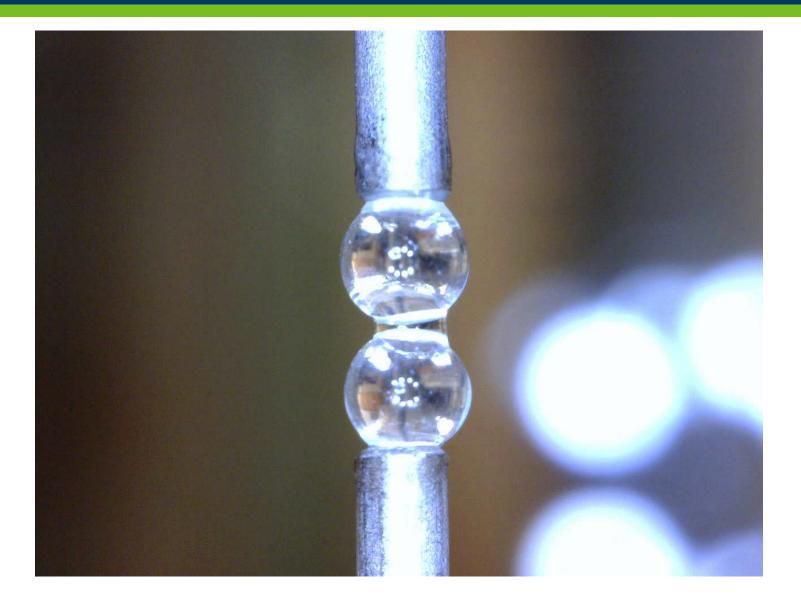
### **Concepts from Interfacial Physics**

- surface tension
- capillarity
- soil-water characteristic curve (SWCC)
- components and units of soil suction

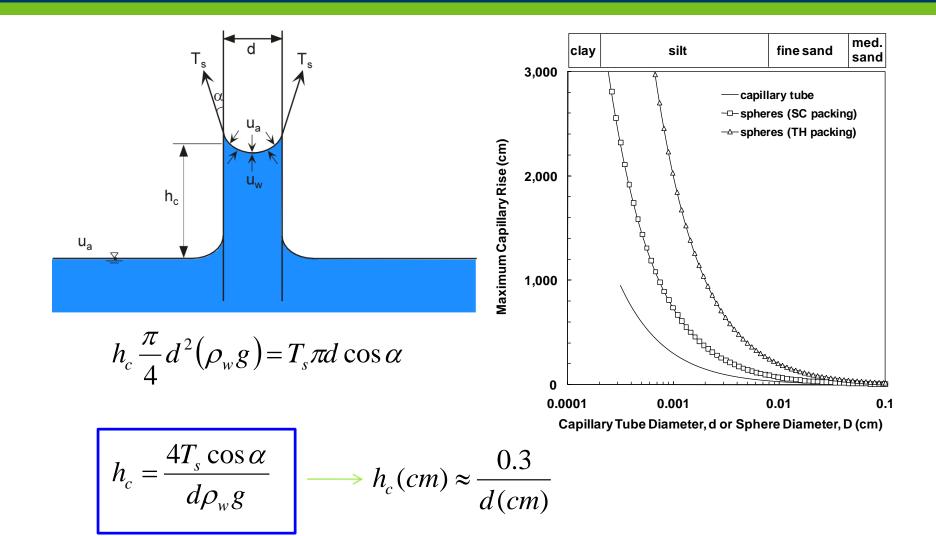
#### Surface Tension, Ts







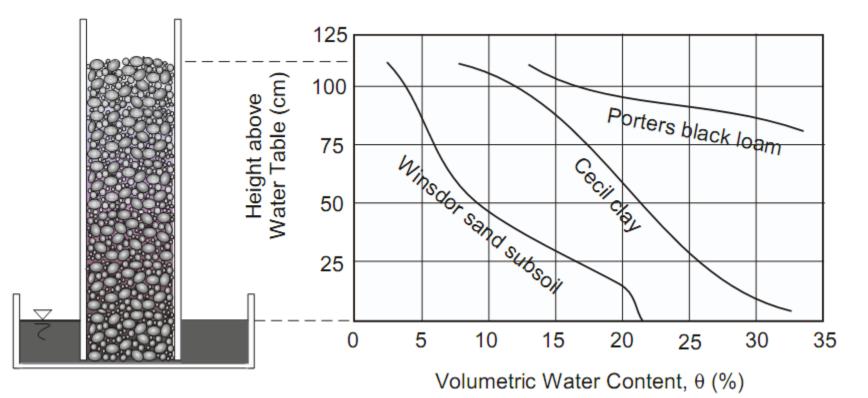
#### Height of Capillary Rise, hc



#### Soil-Water Characteristic Curve (SWCC)

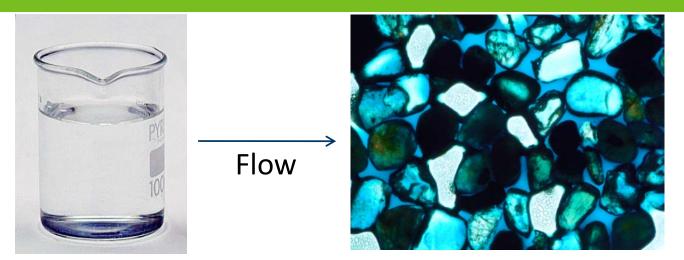
a.k.a. Water Retention Curve (WRC) Capillary Pressure – Saturation Curves (P<sub>c</sub>-S) etc...

(Buckingham, 1907)



(Lu and Likos, 2004)

#### **Components of Soil Suction** Pore Water Potential, $\mu$ (energy per unit mass of water)

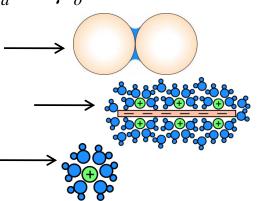


Free Water,  $\mu_i$ 

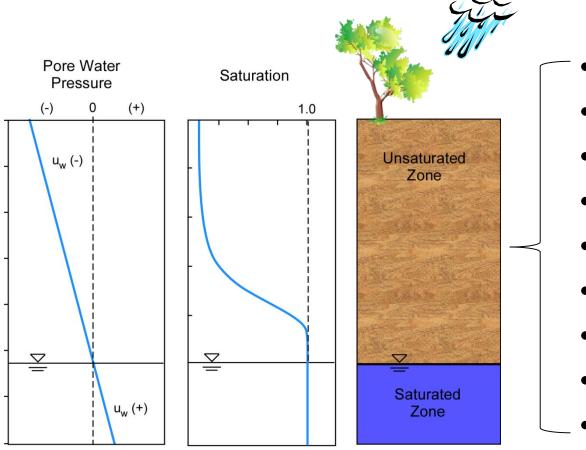
Soil Water,  $\mu < \mu_i$ 

Total change in potential:  $\Delta \mu_t = \Delta \mu_c + \Delta \mu_a + \Delta \mu_o$ 

- $\Delta \mu_c$ : Reduction from capillary effects
- $\Delta \mu_a$ : Reduction from adsorptive effects
- $\Delta \mu_o$ : Reduction from osmotic effects

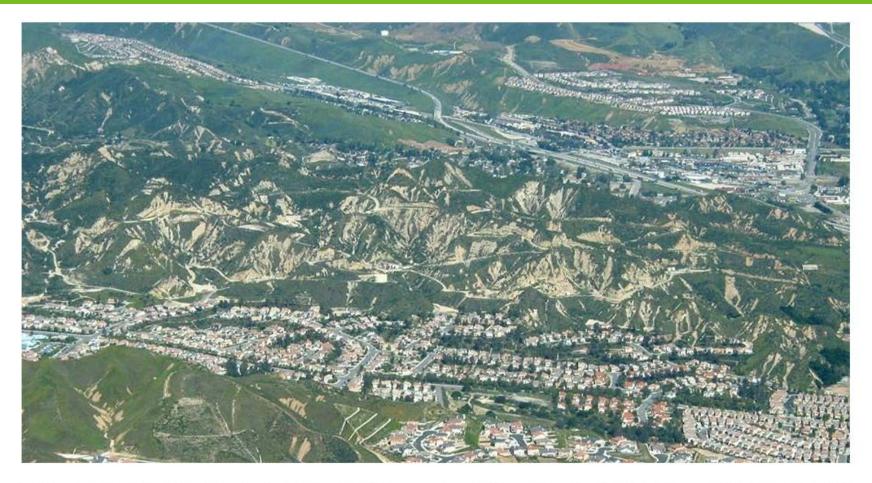


#### Unsaturated soils in geotechnical engineering



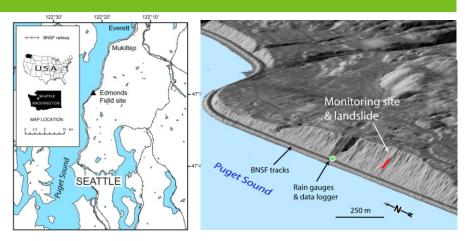
- slopes
- compacted soils
- retaining walls
- excavations
- expansive soils
- shallow foundations
- pavement subgrades
- waste covers
- thermal backfills

#### Precipitation-induced landslides

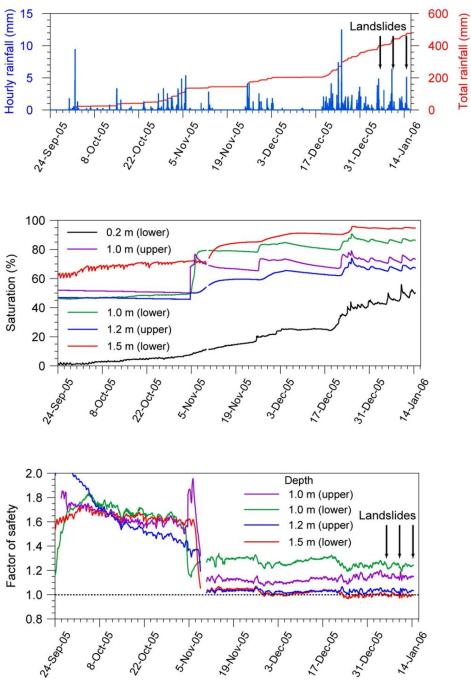


Photograph showing abundant shallow landslides near Valencia, California. The un-vegetated scars are shallow failures caused by heavy rainfall in the winter of 2005. The internal stress-suction stress changes only a few kPa!

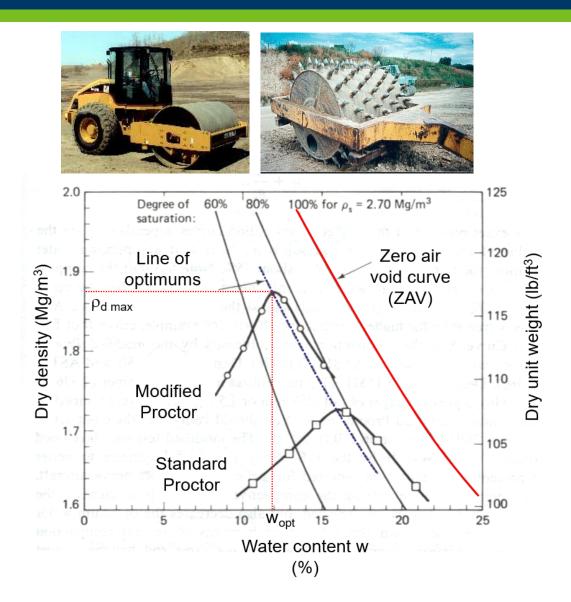
## Landslide Case History: Edmonds WA (2006)

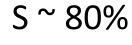


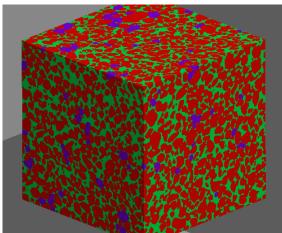




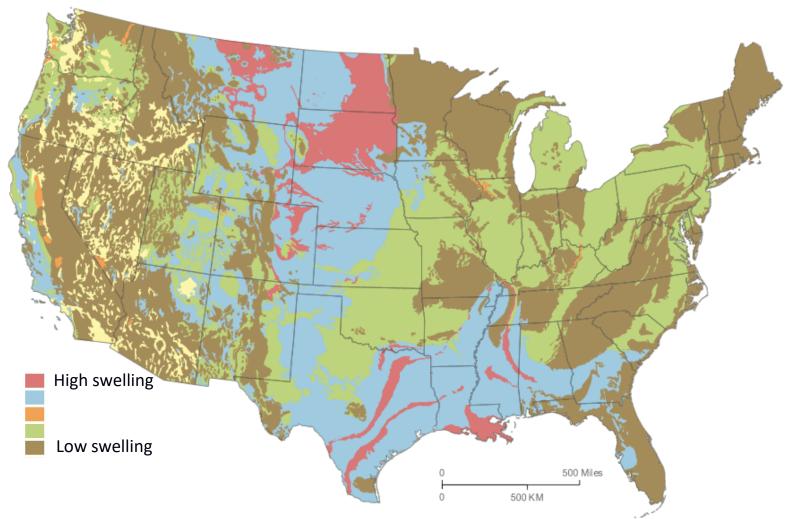
#### Soil Compaction







#### **Expansive Clays**



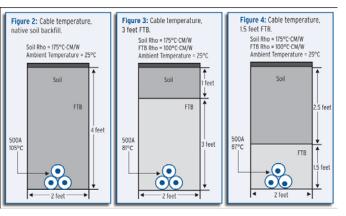
© Geology.com

Source: Geology.com – "Swelling Clays Map of the Conterminous United States" (Olive et al.)

## **Thermal Geotechnics**



#### Buried high-voltage power cables







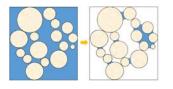
Shallow geothermal

systems



#### Geosynthetic heat exchangers

"energy" piles



#### Measurement of Unsaturated Properties Pavement Applications

#### Raul Velasquez P.E. Ph.D. MnDOT

#### NRRA Webinar May 19, 2020









## Measurement of Unsaturated Properties Pavement Applications

#### 1. Soil Water Characteristic Curve (SWCC)

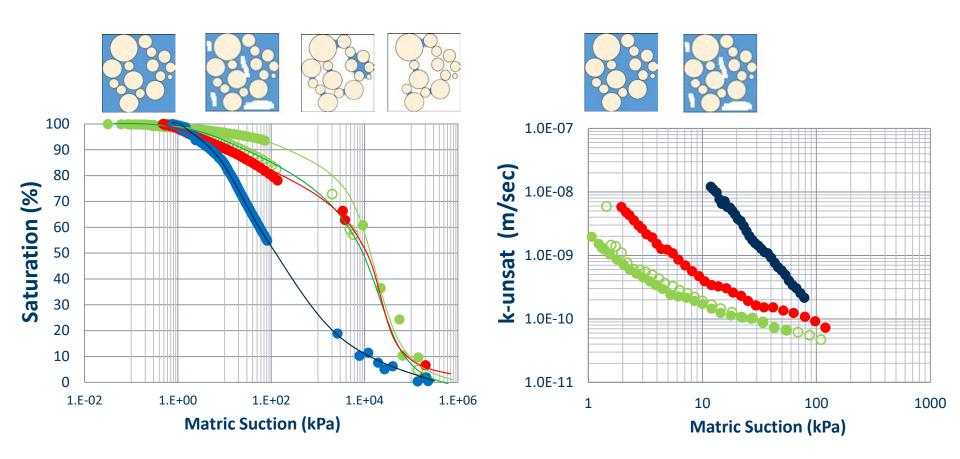
- Tensiometers
- Axis Translation Techniques (Pressure Plates)
- Humidity Measurement Techniques
- Filter Paper Techniques

#### 2. Unsaturated Hydraulic Conductivity (*k-unsat or HCF*)

#### 3. Models for *SWCC* and *k*-unsat

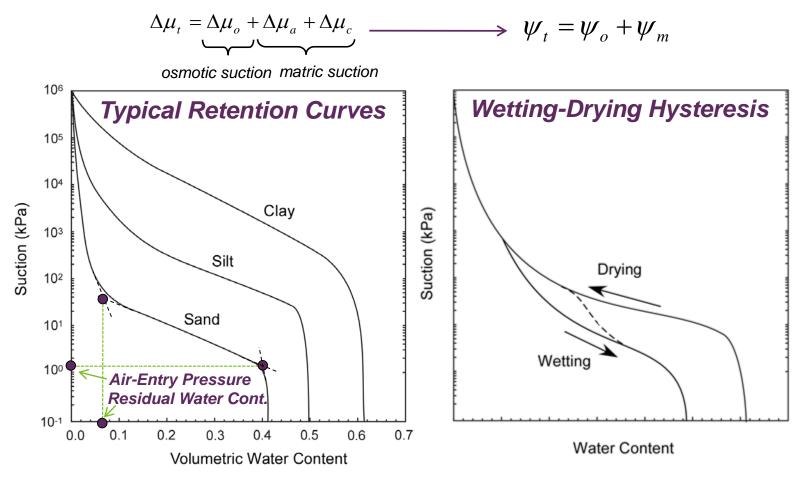
- SWCC
  - Brooks and Corey (BC) Model
  - van Genuchten (VG) Model
  - Fredlund and Xing (FX) Model
- k-unsat
  - Empirical and Macroscopic Models
  - Statistical Models

#### Measurement of Unsaturated Properties Pavement Applications

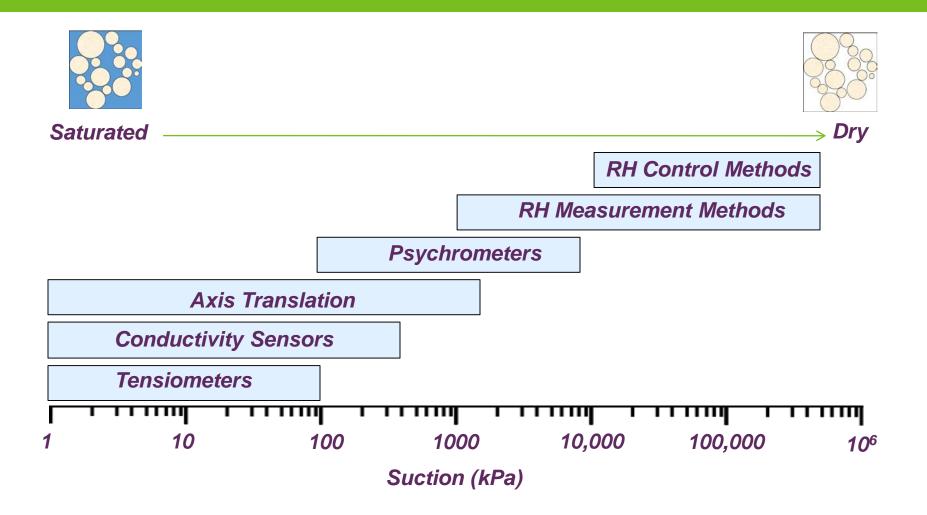


#### Soil Water Characteristic Curve (SWCC)

- Common to express as a pressure potential (suction)
- Energy per unit volume,  $\psi$  (J/m<sup>3</sup> = N/m<sup>2</sup> = Pa)
- Lump total suction into matric and osmotic components



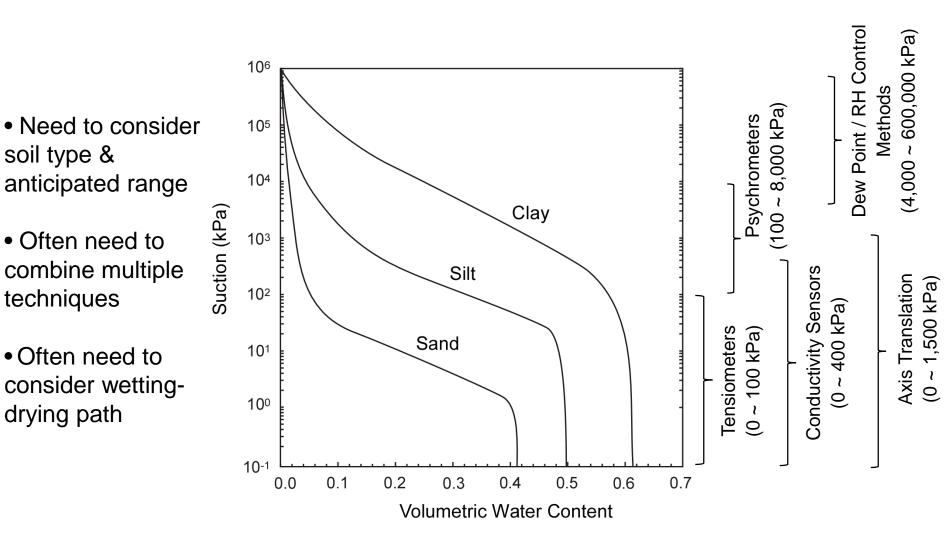
#### Soil Water Characteristic Curve (SWCC)



#### Soil Water Characteristic Curve (SWCC)

Component	Technique/Sensor	Range (kPa)	Principle	Applications
Matric	Tensiometers	0 - 100	Measurement of negative pressure	Lab/Field
Suction	Axis Translation	0 - 1500	Elevated air pressure	Lab
(ψ <sub>m</sub> )	Conductivity Sensors	0 - 400	Therm. cond. material in contact	Lab/Field
	Contact Filter Papers	50 - 100,000	Sorption of filter paper in contact	Lab/Field
Total	Psychrometers	100 - 8,000	RH meas. by dew point method	Lab/Field
	Chilled-Mirror Hygrometers	1,000 - 500,000	RH meas. by dew point method	Lab
	Capactitance Sensors	1,000 - 500,000	RH meas. by polymer sensor	Lab/Field
Suction	Non-contact Filter Papers	1,000 - 500,000	RH meas. by filter paper not in contact	Lab/Field
	Osmotic Humidity Control	10 - 50,000	RH control using salt solutions	Lab
	Flow-Through RH Control	10,000 - 500,000	RH control using controlled gas flow	Lab
	Dynamic Dew Point Method	10,000 - 500,000	Hybrid RH control/meas. method	Lab

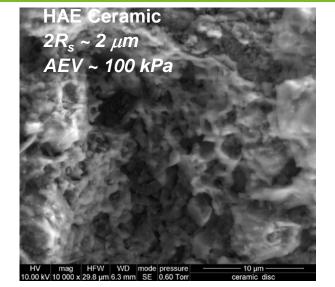
#### Selecting Proper Technique

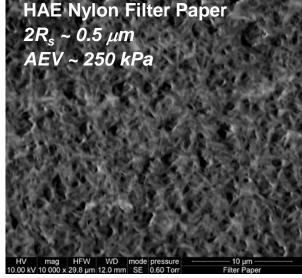


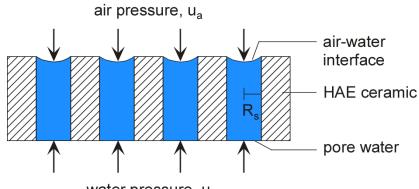
#### High-Air-Entry (HAE) Materials



(Image: Envco)







Type of HAE Ceramic	Approx. Pore Diameter $(\times 10^{-3} \text{ mm})$	Saturated Hydraulic Cond. (m/s)	Air-Entry Value (kPa)
1/2 bar high flow	6.00	$3.11 \times 10^{-7}$	48-62
1 bar	1.70	$7.56 \times 10^{-9}$	138-207
1 bar high flow	2.50	$8.60 \times 10^{-8}$	131-193
2 bar	1.10	$6.30 \times 10^{-9}$	262-310
3 bar	0.70	$2.50 \times 10^{-9}$	317-483
5 bar	0.50	$1.21 \times 10^{-9}$	550
15 bar	0.16	$2.59 \times 10^{-11}$	1520

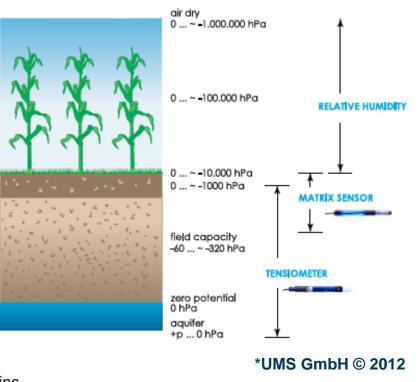
Source: Soilmoisture Equipment Corp. (2003).

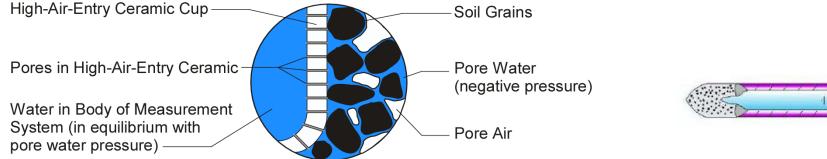
water pressure, u<sub>w</sub>

$$\left(u_a - u_a\right)_b = \frac{2T_s}{R_s}$$

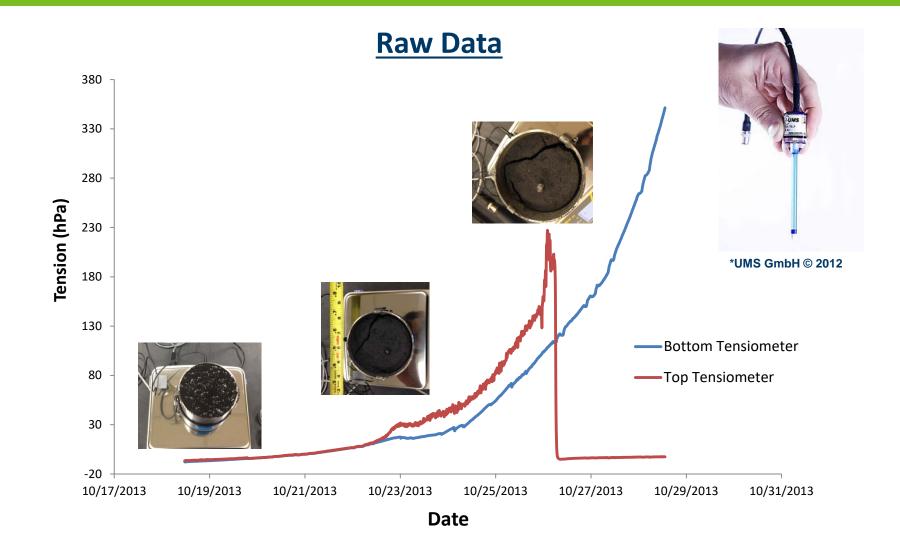
### SWCC - Tensiometers

- Direct measurement of negative u<sub>w</sub>
- Requires exchange of water
- Response time ~ 1-10 min
- Sensors require servicing
- Limited to  $\psi_m \sim 100 \text{ kPa}$



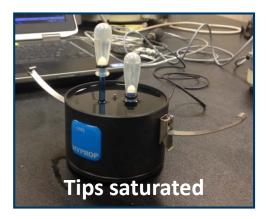


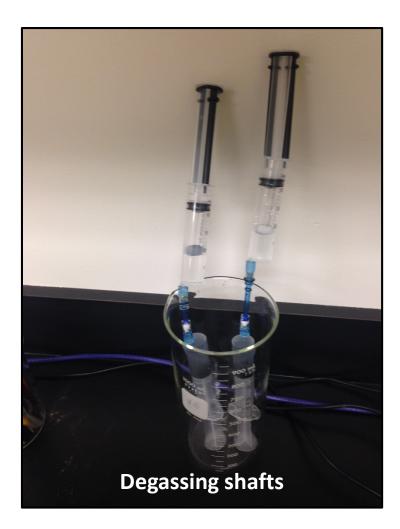
### SWCC - Tensiometers



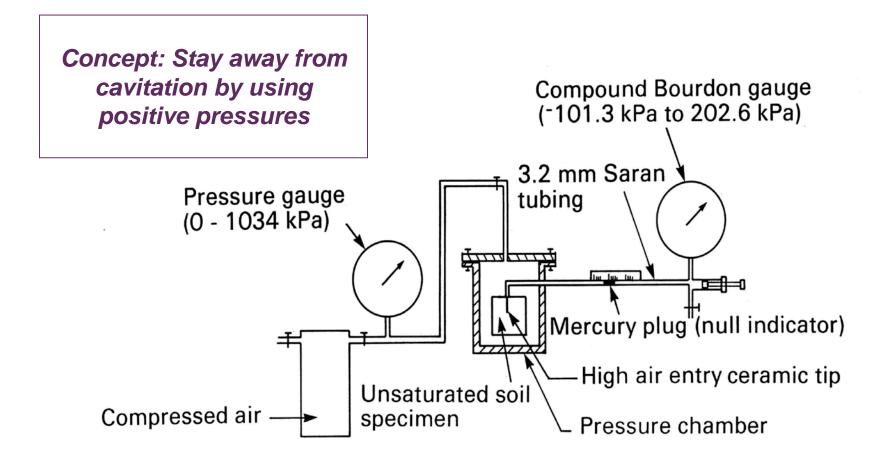
### SWCC – Tensiometers Issues





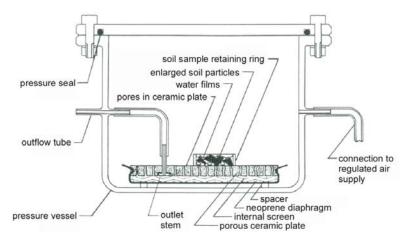


### SWCC – Axis Translation Techniques



Original set up for the null type, axis-translation device for measuring negative pore-water pressure (from Hilf, 1956)

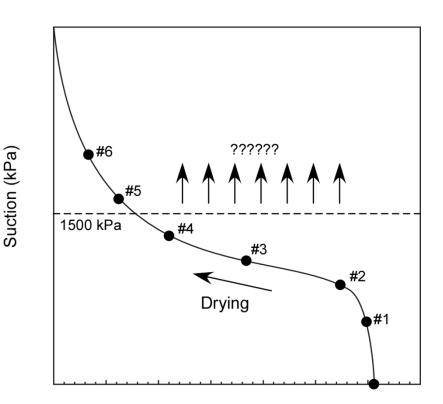
# SWCC – Axis Translation Techniques <u>Pressure Plate</u>



#### \*Soilmoisture Equipment Corp



- Multiple "identical" specimens
- Combine to construct SWCC
- $\Psi_{max}$  ~ 1500 kPa
- Caution beyond residual suction!



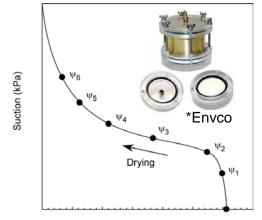
#### Water Content

# SWCC – Axis Translation Techniques <u>Tempe Cell System</u>

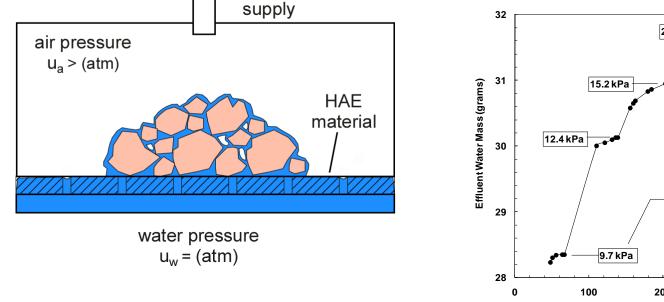
- Elevated air pressure and HAE material
- Matric suction,  $\psi_m = (u_a u_w)$
- Single specimen, primarily drainage path

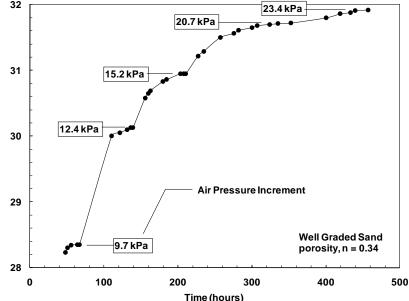
air pressure

- Typically back-calculate S from effluent
- Range: ~ 100 kPa (sands)

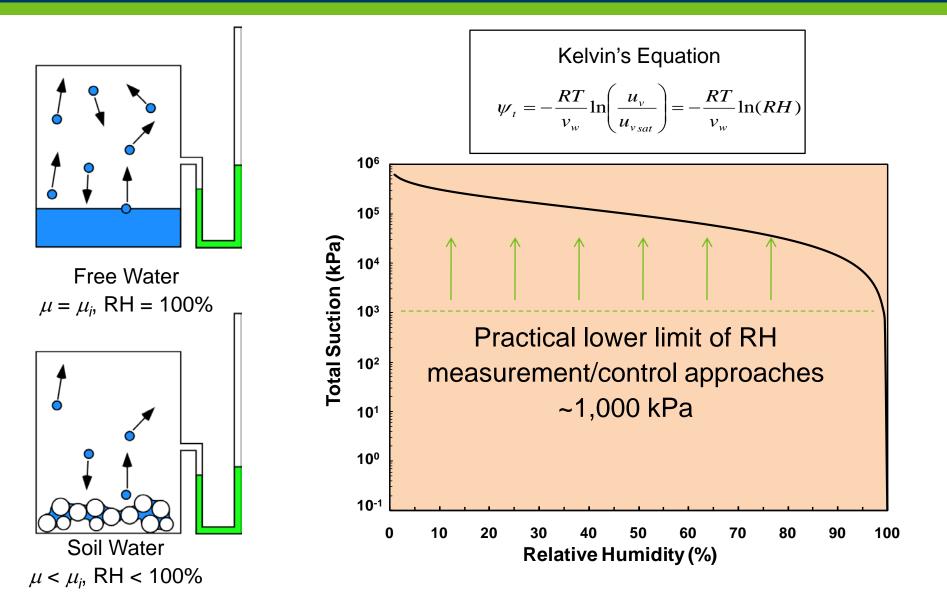








### SWCC- Humidity Measurement Techniques



### SWCC- Humidity Measurement Techniques Dew Point Methods

Water potential=> measurement of energy status of water in a soil. It indicates how tightly water is bound structurally or chemically

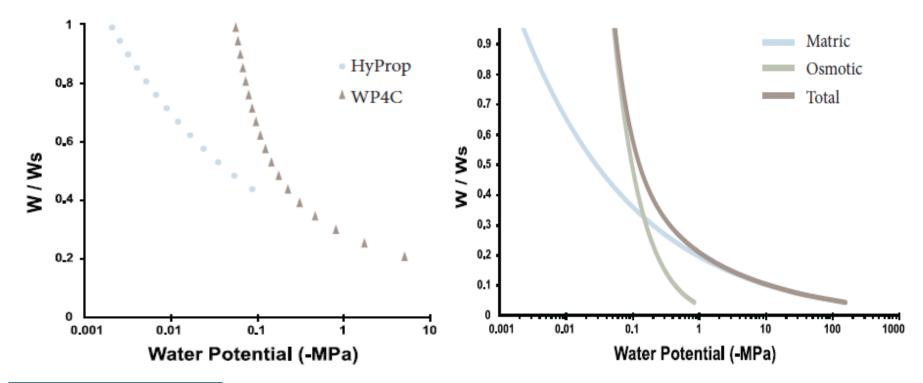
WP4c=> uses the chilled mirror dew point technique (ASTM 6836 Method D)

<u>Water potential</u> can be computed from vapor pressure of air in <u>equilibrium</u> with soil sample in a sealed chamber





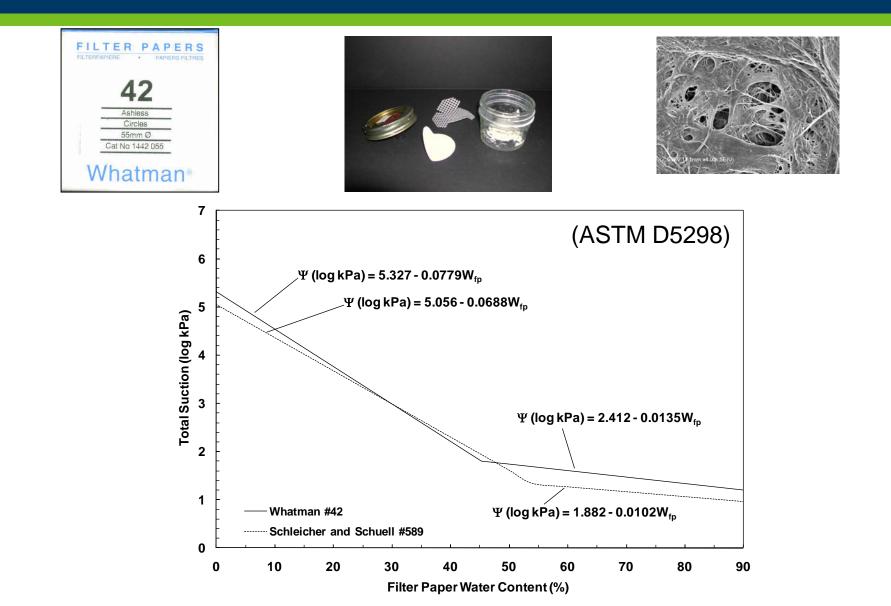
### WP4C Measure Osmotic and Matric Components of Water Potential



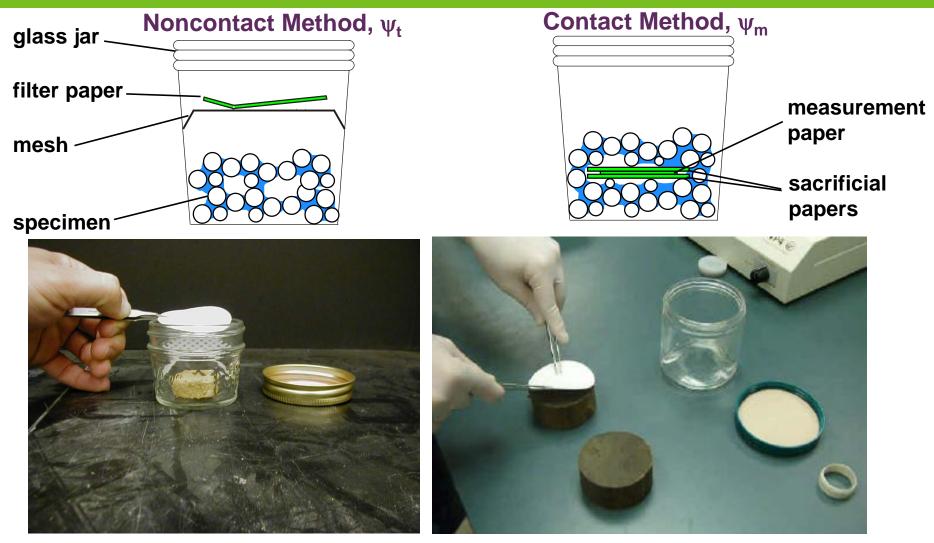


\*Decagon (2013), How to Create a Full Moisture Release Curve Using the WP4C and HyProp, Inc, Pullman, WA.

### SWCC- Filter Paper Techniques

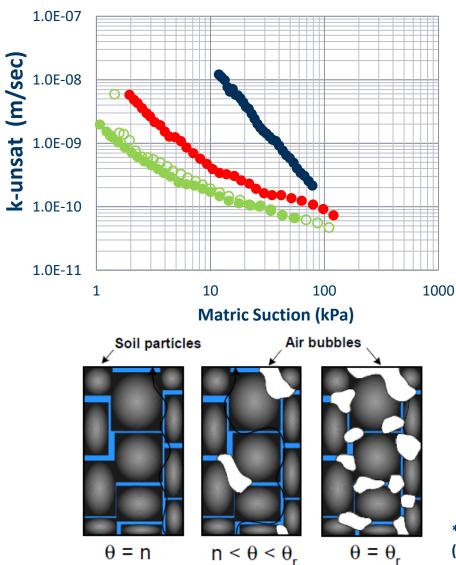


### SWCC- Filter Paper Techniques



\*Lytton and Bulut, 2003

### Unsaturated Hydraulic Conductivity (k-unsat or HCF)



\*Seepage Modeling with SEEP/W, (2012), GEO-SLOPE International, Ltd.

# Unsaturated Hydraulic Conductivity (*k-unsat*)



- <u>Mostly estimated/calculated</u> from k-sat and SWCC
- Alternatively =>evaporation method with two tensiometers:

$$q^{i} = \frac{1}{\beta} \left( \frac{\Delta V^{i}}{\Delta t^{i}} A \right)$$

 $q^i$  = water flow at evaluation point *i* 

 $\Delta V^i$  = water loss determined by weight changes at evaluation point *i* 

 $\Delta t^i$  = time interval between two measurement points

A = cross sectional area

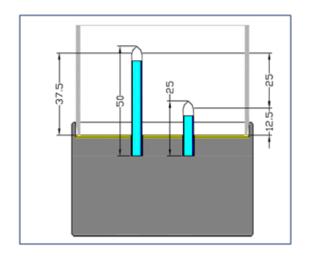
 $\beta$  = geometry coefficient (standard  $\beta$ =2)

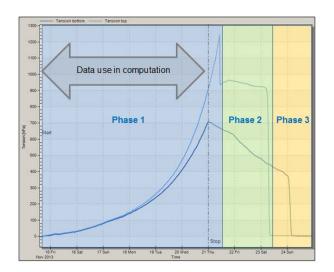
### Unsaturated Hydraulic Conductivity (*k-unsat*)

Darcy's law:

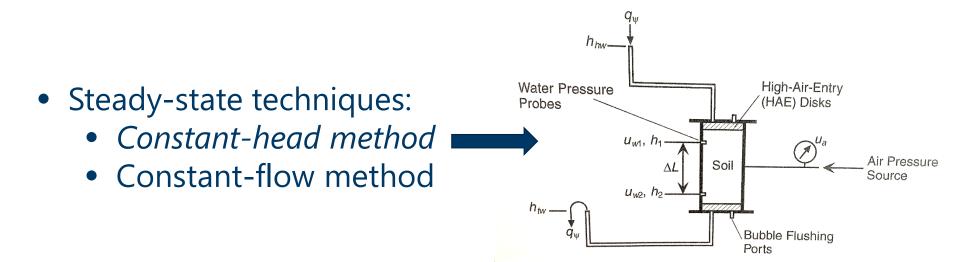
$$K_{unsat}^{i}(\Psi) = -\frac{q^{i}}{\Delta h^{i}/_{\Delta z} + 1}$$

 $K_{unsat}^{i}$  = unsaturated hydraulic conductivity at evaluation point *i*   $\Psi$  = average suction between two measurement points in time  $\Delta h^{i}$  = difference in water tension between tensiometers at evaluation point *i*  $\Delta z$  = distance between tensiometers tips





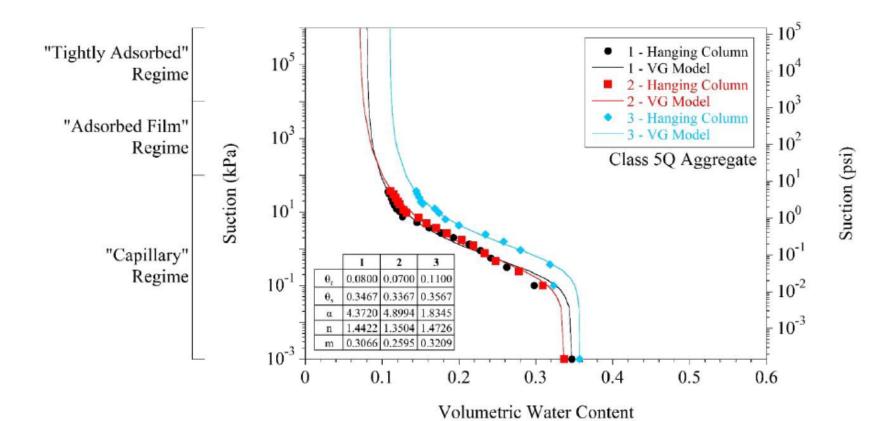
# Unsaturated Hydraulic Conductivity (k-unsat)



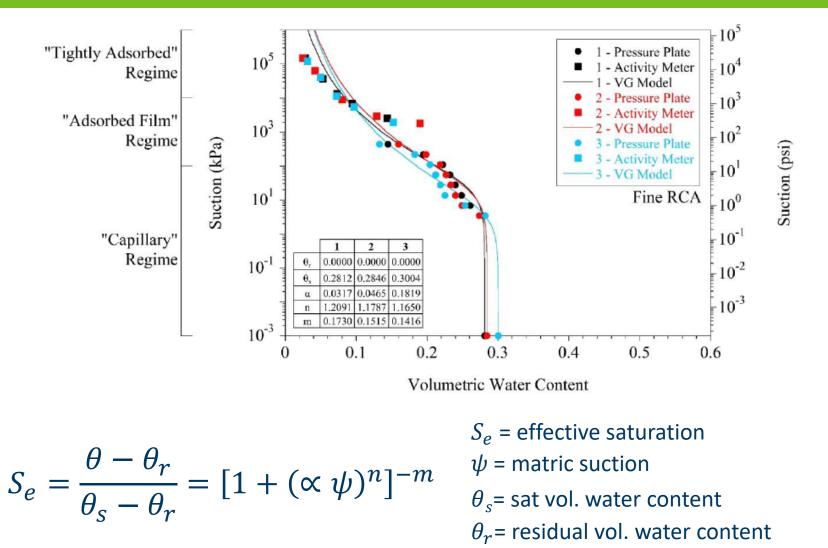
- Transient techniques (*hydraulic diffusivity*):
  - Horizontal infiltration method
  - Outflow methods
  - Instantaneous profile methods
    - Lab
    - Field

### Common Models for SWCC

- Brooks and Corey (BC) Model
- van Genuchten (VG) Model
- Fredlund and Xing (FX) Model



# Common Models for *SWCC* van Genuchten (VG)

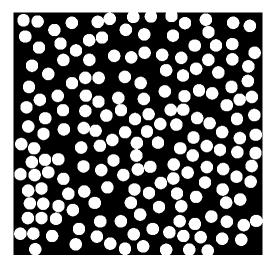


 $\propto$ , *n*, *m* = empirical fitting parameters

### Common Models for *k-unsat (HCF)*

- Empirical and Macroscopic Models
- Statistical Models
  - van Genuchten (VG) Model
  - Fredlund Model

**Basis of Statistical Modeling** 



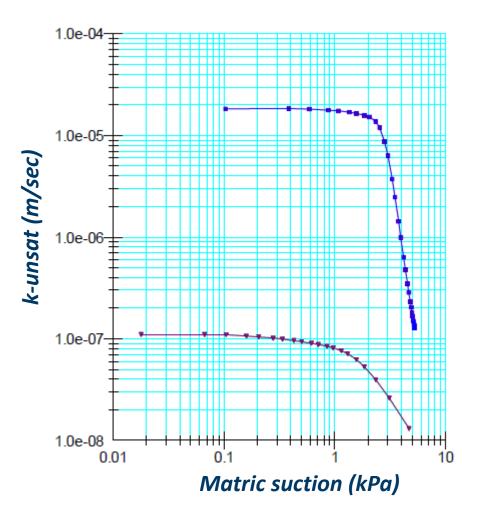
Randomly sized and randomly distributed pores

### Common Models for *k-unsat (HCF)* van Genuchten (VG)

$$k_{w} = k_{s} \frac{\left[1 - \left(a\Psi^{(n-1)}\right)\left(1 + \left(a\Psi^{n}\right)^{-m}\right)\right]^{2}}{\left(\left(\left(1 + a\Psi\right)^{n}\right)^{\frac{m}{2}}\right)}$$

- $k_s$  = saturated hydraulic conductivity  $\psi$  = matric suction
- $a = m = \text{ompirical fitting paran$
- a, n, m = empirical fitting parameters

$$n = \frac{1}{1 - m}$$



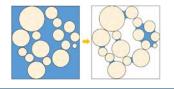
\*Seepage Modeling with SEEP/W, (2012),GEO-SLOPE International, Ltd.

# **Closing Remarks**

- Suction spans a range over 6 orders of magnitude
- No single measurement technique is ideal for every application
- Measurement approach must consider:
  - Soil type
  - Range of wetting
  - Wetting direction
  - Applicability in the lab or field
- Quality measurements require careful protocol and calibration

### Acknowledgments

Material from W. Likos (UW-Madison) and M. Padilla (GCTS Testing Systems), ASCE 2011 Webinar



### Q&A - Fundamentals

### All

#### NRRA Webinar May 19, 2020



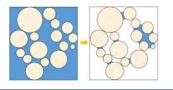






# Break (10 min)

- Welcome Introduction *T. Beaudry*
- Fundamental Concepts in Unsaturated Soil W. Likos
- Measurement of Unsaturated Properties R. Velasquez
- Q&A Fundamentals All
- <u>Break (10 min)</u>
- Impact of Moisture on Pavement Foundation Materials *B. Cetin*
- Importance of Unsaturated Soil Mechanics in ME Design *B. Cetin*
- Correlations between Unsat Soil Parameters and ME Design Input B. Cetin
- Use of Unsaturated Soil Mechanics by MnDOT- J. Siekmeier
- Q&A Applications All
- Closing Remarks *T. Beaudry*



### Impact of Moisture on Pavement Foundation Materials

#### Bora Cetin, PhD

Assistant Professor Michigan State University <u>cetinbor@msu.edu</u>

#### NRRA Webinar May 19, 2020







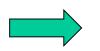


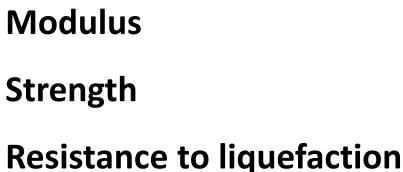
# COMPACTION

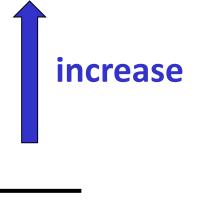
- Compaction is the <u>densification</u> of a soil by the use of <u>mechanical</u> energy
  - The process of expelling <u>air</u> from the soil
  - Improves strength
    - Increases bearing capacity of foundations
    - Increases <u>stability</u> of embankment slopes
  - Reduces compressibility
    - Decreases <u>settlement</u> of foundations
  - Reduces permeability

# **Compaction Principles**

• The basic principle of densification is the re-arrangement of particles into a denser state, which results in





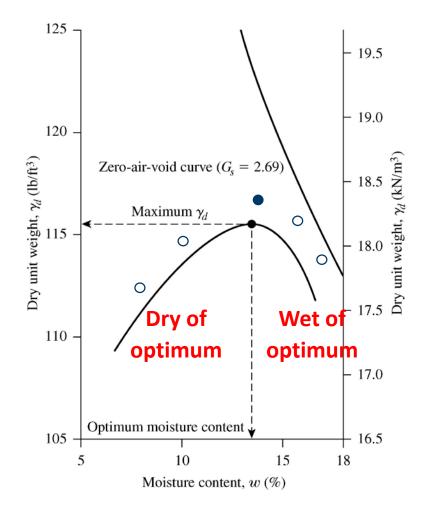


Permeability

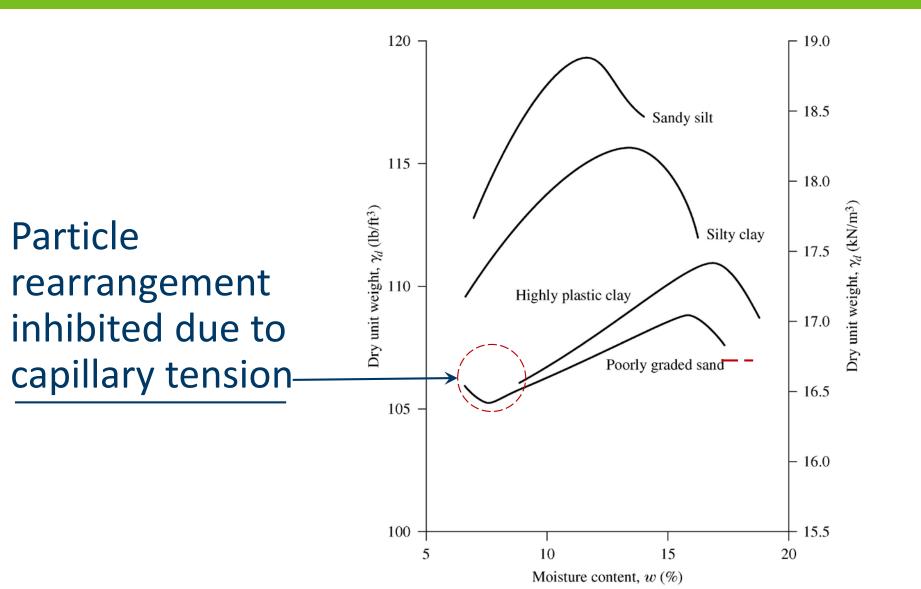
Collapsibility



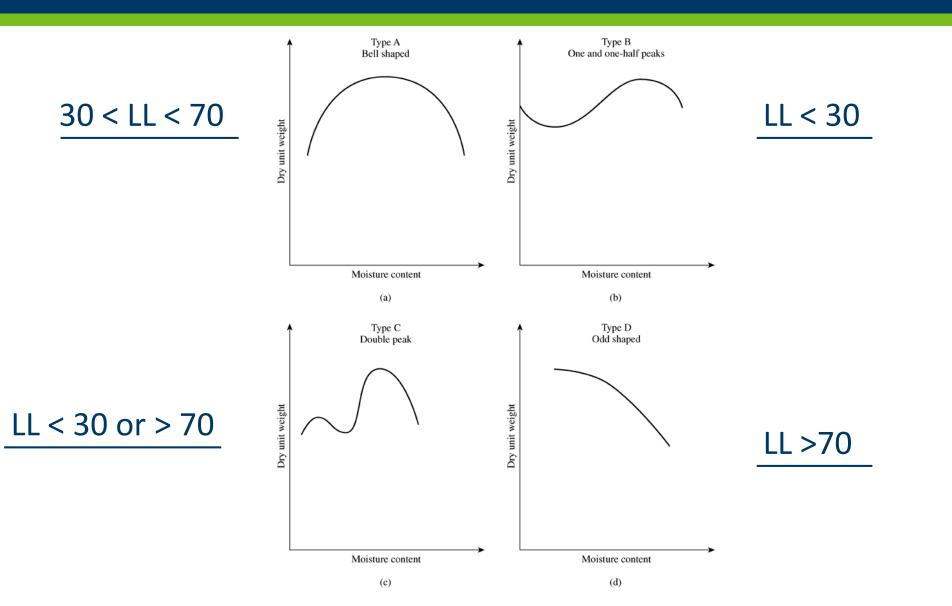
### Dry Unit Weight vs. Moisture Content Curve



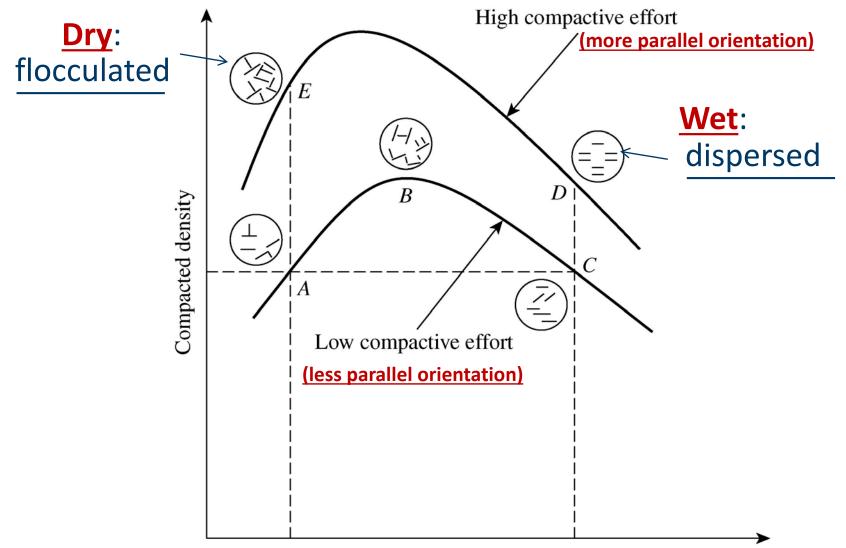
# Effect of Soil Type



# Types of compaction curves



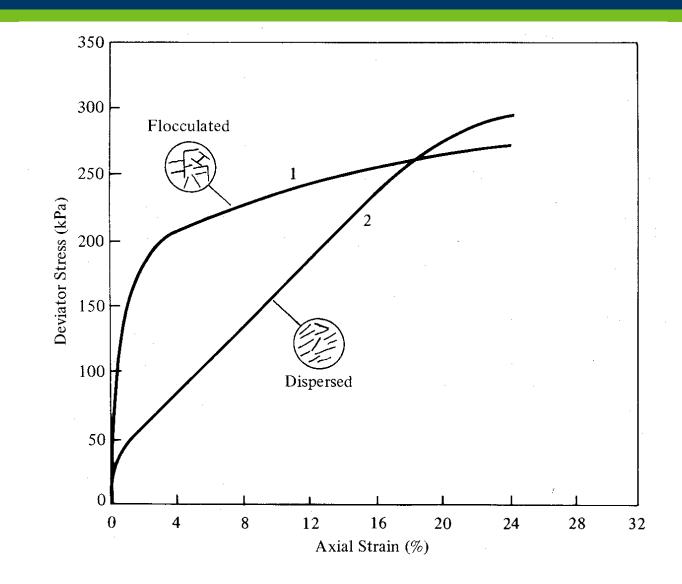
# STRUCTURE OF COMPACTED CLAY SUBGRADE WITH MOISTURE



Molding water content

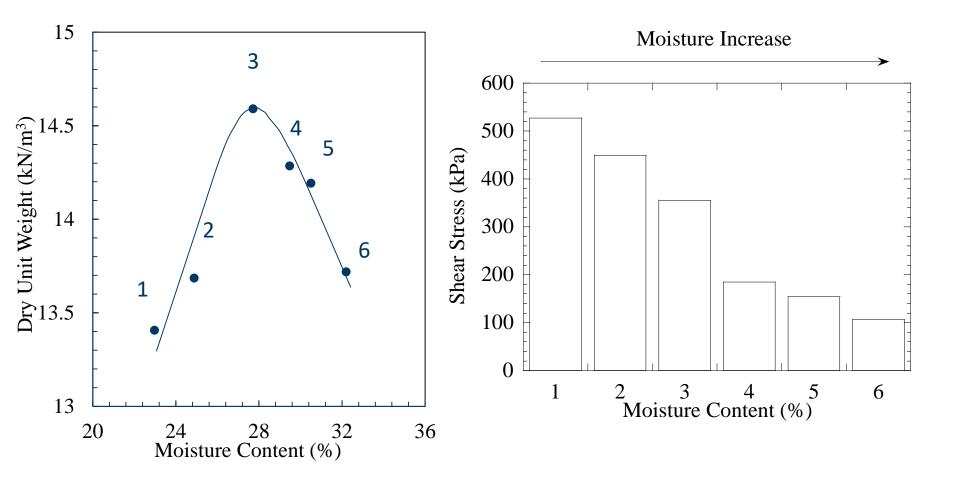
# Effect of Moisture on Soil Properties

Stress-Strain and strength



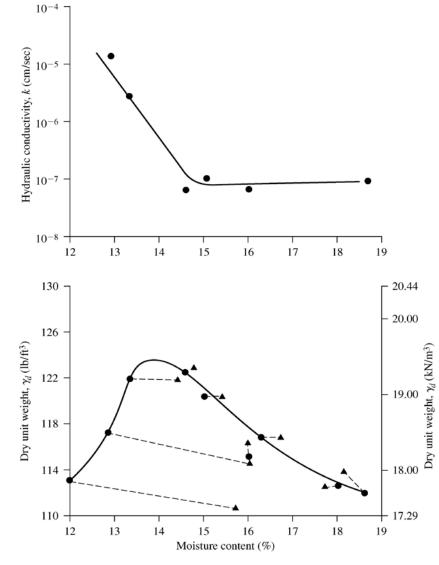
# Effect of Moisture on Soil Properties

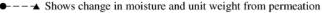
### Stress-Strain and strength



# Effect of Compaction on Soil Properties

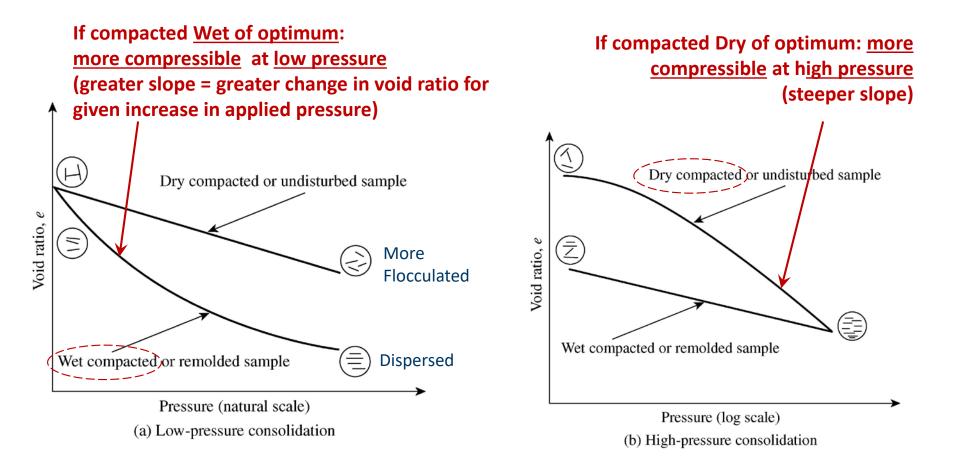
# Permeability





### EFFECT OF MOISTURE ON SOIL PROPERTIES

#### **Compressibility / Settlement**



### EFFECT OF MOISTURE ON SOIL PROPERTIES

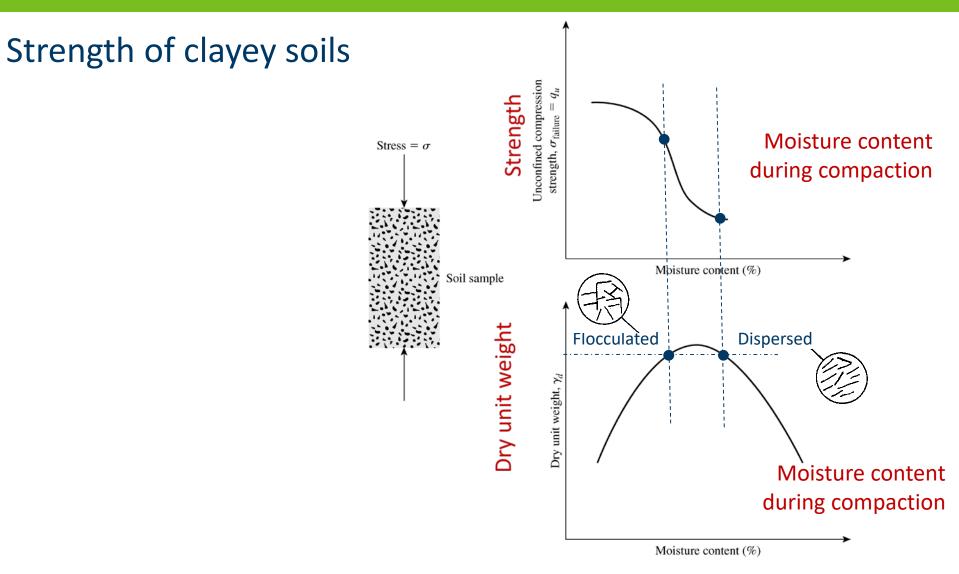
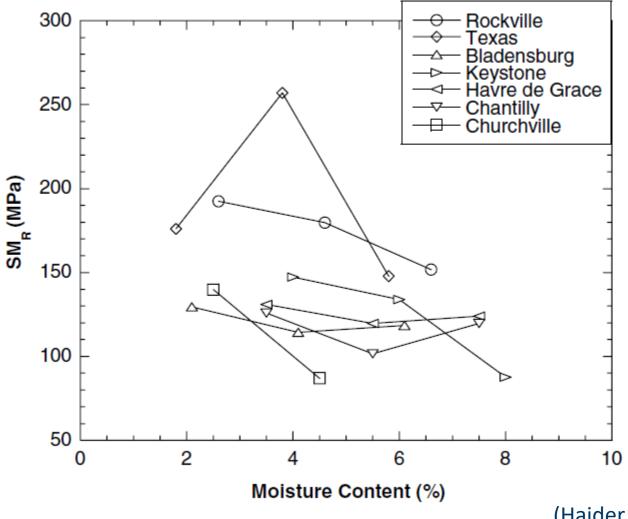


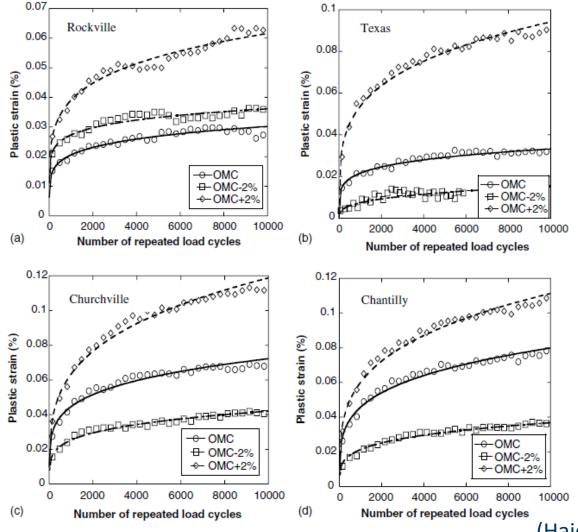
Figure 5.18 Effect of compaction on the strength of clayey soils

### Effect of Moisture Content on Resilient Modulus of Granular Aggregate Base Materials



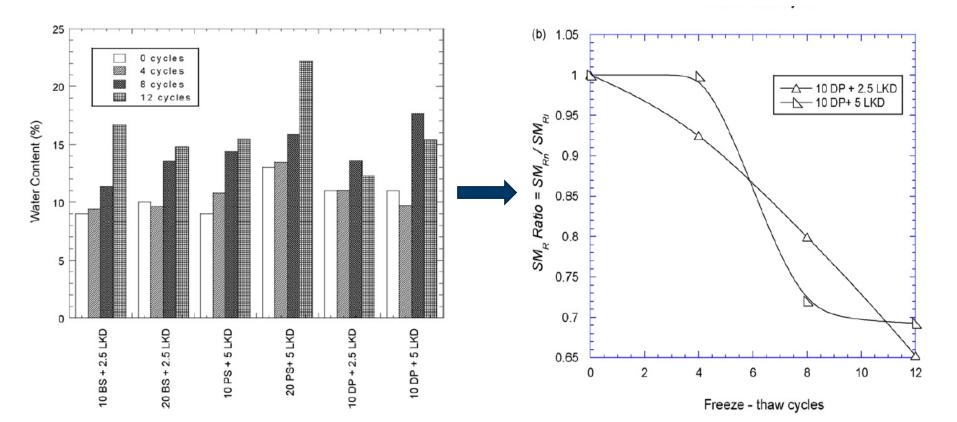
(Haider et al. 2014)

### Effect of Moisture Content on Permanent Deformation of Granular Aggregate Base Materials



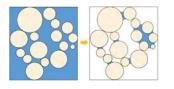
(Haider et al. 2014)

### Effect of Freeze-Thaw Cycles on Moisture/Resilient Modulus



BS: Brandon Shores Power Plant Fly Ash PS: Paul Smith Power Plant Fly Ash DP: Dickerson Precipitator Plant Fly Ash LKD: Lime Kiln Dust

(Cetin et al. 2010)



### Importance and Integration of Unsaturated Soil Mechanics in Pavement M-E Design

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#### NRRA Webinar May 19, 2020



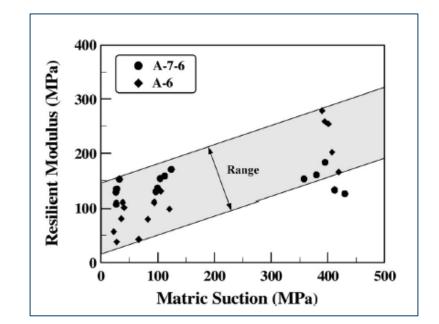






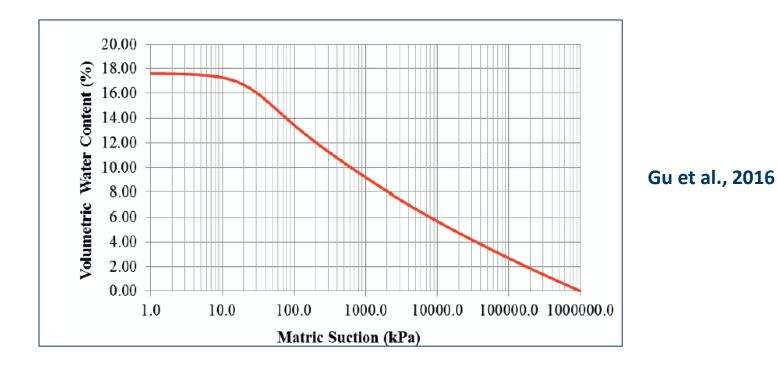
- Having unsaturated geomaterials in the pavement foundation leads many researches to focus on the behavior of the unsaturated geomaterials by investigating the relationship between:
- Saturation degree versus matric suction
- Shear strength versus matric suction
- Stiffness (Resilient Modulus) versus

matric suction



(Yang et al. 2008)

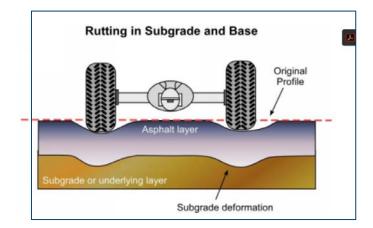
• Matric suction in a pavement structure changes as water content changes.



- The increase in the matric suction has a significant effect on the shear strength and modulus of geomaterials in the pavement and it is directly related to:
  - Total Rutting: Shear strength directly affects total rutting; it decreases as shear strength increases



Rutting failure due to the weak shear strength of subgrade



**Colorado Department of Transportation 2017 Pavement Design Manual** 

• Load-related Cracking (Alligator and Longitudinal): A larger shear strength and modulus improve the integrity of supporting layers and also resistance to load-related cracking

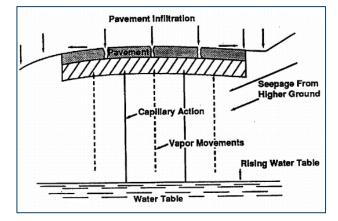


#### **Alligator cracking**

• Smoothness (IRI): High shear strength and modulus result in low IRI values

 Environmental conditions such as precipitation, change in the water table level and drainage conditions, causing distress to the pavement by changing the moisture content matric suction





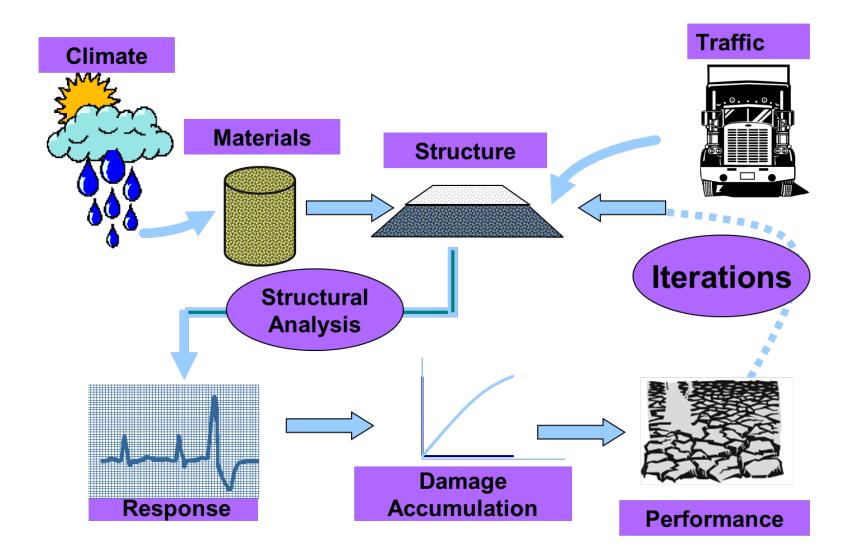


**Climate conditions** 

Sources of Subsurface Water in Pavements

**Drainage quality** 

# Pavement M-E Design



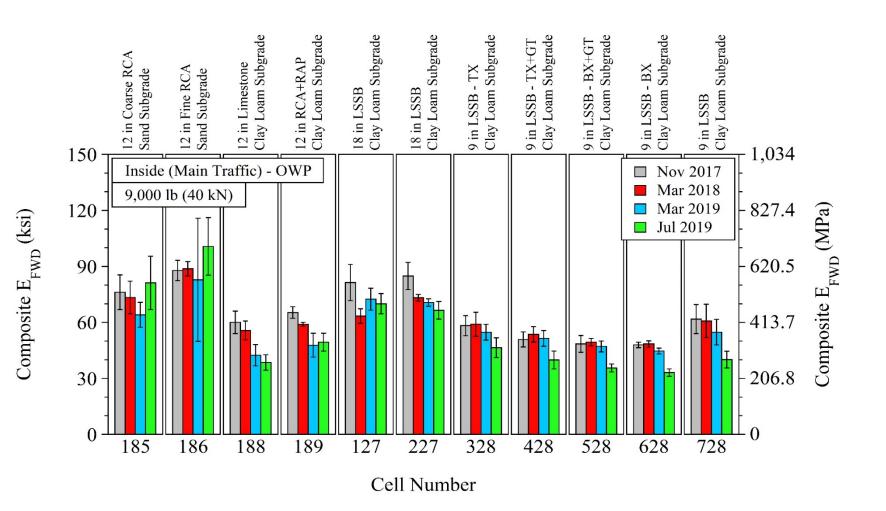
## Pavement ME Design Guide Features

- Hierarchical approach to inputs
- Axle load spectra data (not ESALs)
- Consideration of climatic effects
- Use of intrinsic material properties
- Consideration of key distress types
- Incremental damage approach

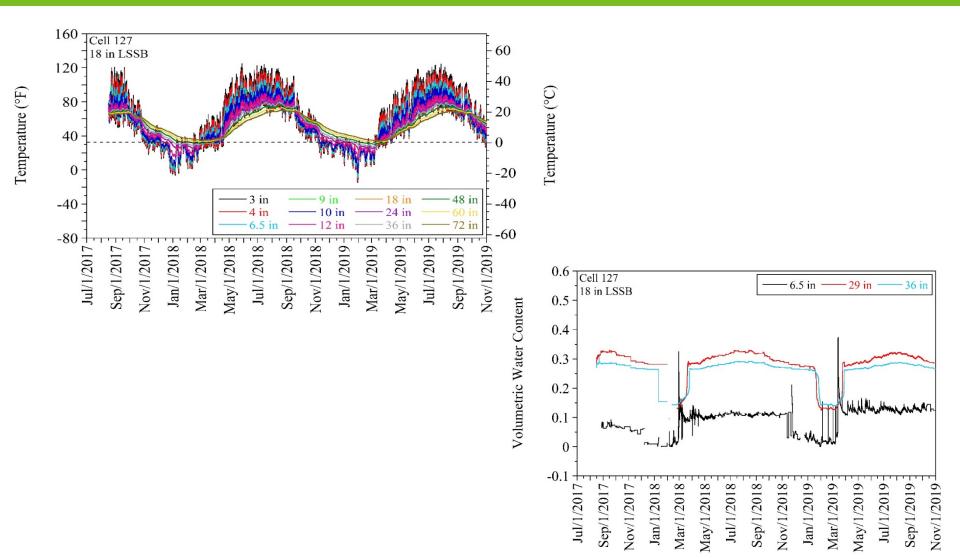
# **Incremental Damage**

- Changes over time are addressed
  - •Material strength and stiffness
  - •seasonal moisture and temperature
  - variations in traffic seasonally and over time

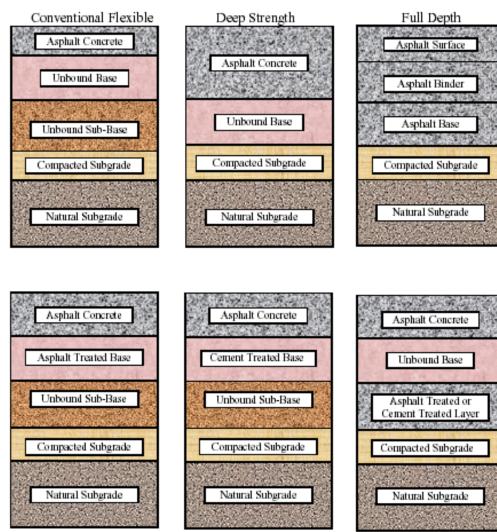
## Incremental Damage/Stiffness



## Incremental Damage/Moisture & Temperature



## **Material Characterization**



Semi-Rigid with ATB

Semi-Rigid with CTB

Inverted Section

## Analysis Procedure in Pavement – ME

### • Step 1 – Input

- Subgrade soil properties, AASHTO classification
- Resilient modulus at reference condition, gradation, engineering and index properties, Atterberg limit tests

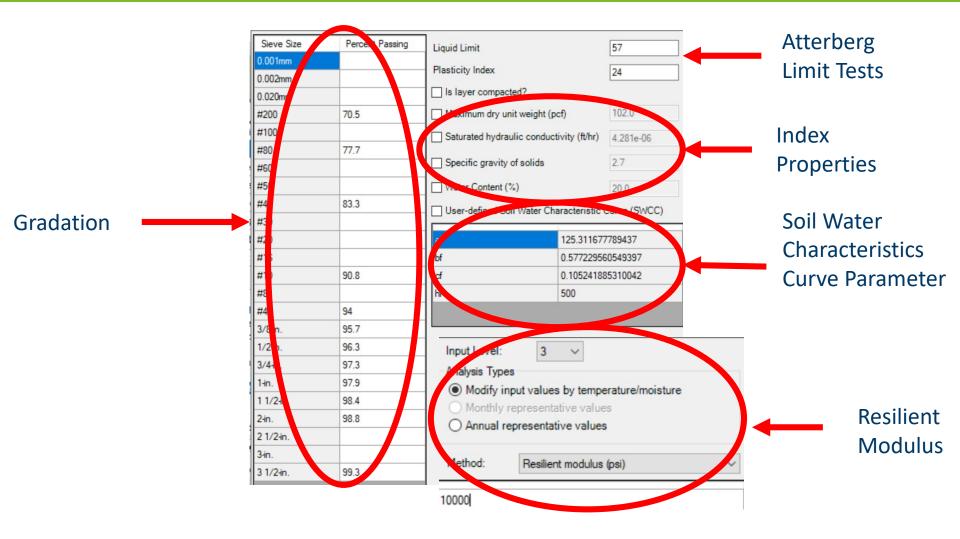
### • Step 2 – Background

• Estimation of adjusted resilient modulus for varying moisture and temperature condition for each month over the design life (i.e. 20 years)

### Step 3 – Distress

• Determination of pavement distress (i.e. cracking, rutting, IRI) for due to seasonal variation in resilient modulus

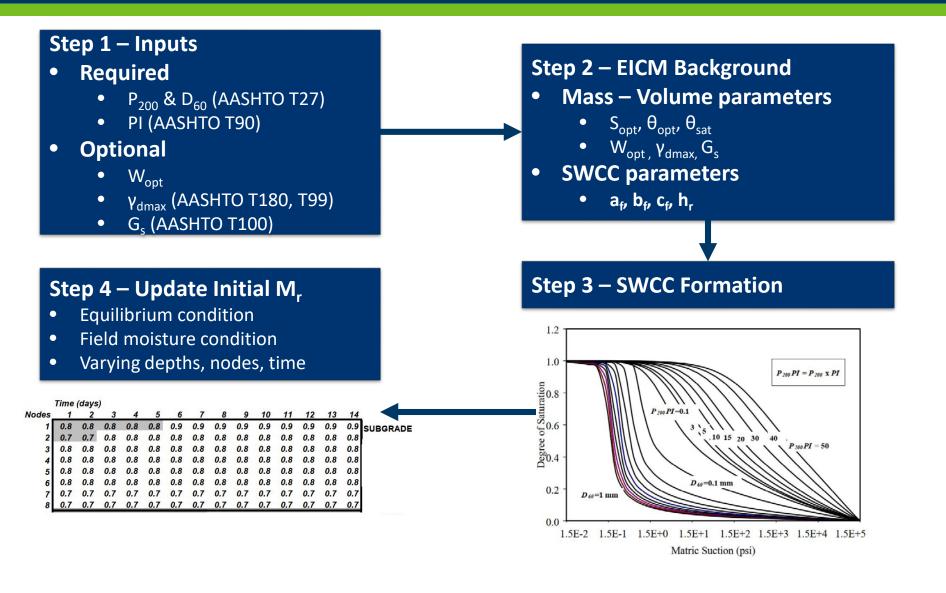
# Subgrade Inputs for Pavement-ME



# Soil Water Characteristics Curve (SWCC)

- SWCC determines the relationship between water content and suction for a given soil.
- Pavement-ME generates the SWCC curve based on four parameters.
  - a<sub>f</sub> (psi)
  - b<sub>f</sub>
  - C<sub>f</sub>
  - h<sub>r</sub> (psi)

# Pavement – ME SWCC Flow Chart



### Enhanced Integrated Climatic Model (EICM)

- 1 dimensional coupled heat and moisture flow program
- Simulates the changes in pavement layers and subgrade due to climatic condition over the years
- Determines Mass Volume parameters, Soil Water Characteristics Curve (SWCC) parameters based on
  - P<sub>200</sub> and P<sub>4</sub> (% passing #200 and #4)
  - D<sub>60</sub> (effective grain size for 60 % passing)
  - PI (plasticity index)

## **Mass-Volume Parameters**

$$S_{opt} = 6.752 * (P_{200} * PI)^{0.147} + 78$$
  

$$G_s = 0.041 * (P_{200} * PI)^{0.29} + 2.65$$
  

$$\gamma_{d \text{(max comp)} = \frac{G_s * \gamma_{water}}{1 + \frac{W_{opt} * G_s}{S_{opt}}}$$

where,

 $G_s$  = Oven dry specific gravity of soil

 $S_{opt}$  = Initial degree of saturation of soil

*P*<sub>200</sub>= % passing #200 sieve

PI = Plasticity Index of soil

 $\gamma_{d (max comp)}$  = Maximum dry unit weight of soil

 $W_{opt}$  = Optimum gravimetric water content of soil

## **Mass-Volume Parameters**

$$\begin{split} W_{opt} &= 1.3 * (P_{200} * PI)^{0.73} + 11 & \text{if } P_{200} * PI > 0 \\ W_{opt} &= 8.6425 * (D_{60})^{-0.1038} & \text{if } P_{200} * PI = 0 \\ \theta_{opt} &= W_{opt} * \gamma_{d \max} \\ \theta_{sat} &= \frac{\theta_{opt}}{S_{opt}} \end{split}$$

where,

 $W_{opt}$  = Optimum gravimetric water content of soil

 $P_{200}$ = % passing #200 sieve

*PI* = Plasticity Index of soil

 $D_{60}$  = Effective grain size for 60% passing

 $\theta_{opt}$  = Optimum volumetric water content

 $\theta_{sat}$  = Saturated volumetric water content

 $\gamma_{d (max comp)}$  = maximum dry unit weight of soil

### Soil-Water Characteristic Curve Parameters

$$a_{f} = \frac{0.00364(P_{200}PI)^{3.35} + 4(P_{200}PI) + 11}{6.895}$$

$$\frac{b_{f}}{c_{f}} = -2.313(P_{200}PI)^{0.14} + 5$$

$$c_{f} = 0.0514(P_{200}PI)^{0.465} + 0.5$$

$$\frac{h_{r}}{a_{f}} = 32.44e^{0.0186(P_{200}PI)}$$

if  $P_{200} * PI > 0$ where,

 $P_{200}$ = % passing #200 sieve PI = Plasticity Index of soil

### Soil-Water Characteristic Curve Parameters

$$a_f = \frac{0.8627(D_{60})^{-0.751}}{6.895}$$
  

$$b_f = 7.5$$
  

$$c_f = 0.1772 \ln(D_{60}) + 0.7734$$
  

$$\frac{h_r}{a_f} = \frac{1}{D_{60} + 9.7e^{-4}}$$

if  $P_{200} * PI = 0$ where,

 $P_{200}$ = % passing #200 sieve PI = Plasticity Index of soil  $D_{60}$  = Effective grain size for 60% passing

### Soil-Water Characteristic Curve Parameters

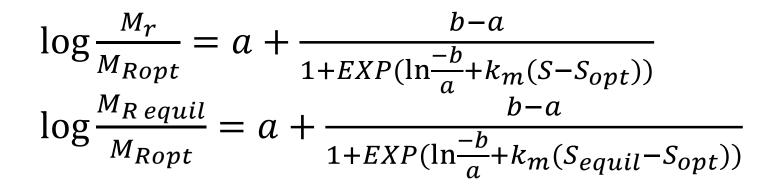
$$S_{equil} = C(h) * \frac{1}{\left(\ln\left(EXP(1) + \left(\frac{h}{a_f}\right)^{b_f}\right)\right)^{c_f}}$$

$$C(h) = 1 - \frac{\ln(1 + \frac{h}{h_r})}{\ln(1 + \frac{1.45 \times 10^5}{h_r})}$$

where,

$$h = y_{GWT} * \gamma_{water}$$
  
 $S_{equil} = Equilibrium degree of saturation$ 

### Effect of Soil Moisture on Resilient Modulus



where,

 $M_r$  = Resilient modulus at a given time

 $M_{Reguil}$  = Equilibrium resilient modulus

 $M_{Ropt}$  = Resilient modulus at a reference condition

 $a, b = Min \& max of log \frac{M_r}{M_{Ropt}}$ 

 $k_m$  = Regression parameter

 $S - S_{opt}$  = Variation in degree of saturation

 The Pavement ME Design incorporated the suction in the MR model through NCHRP Project 9-23A:

$$M_{R} = k_{1}P_{a}\left(\frac{\theta + wc * matric \_suction}{P_{a}}\right)^{k_{2}}\left(\frac{\tau_{oct}}{P_{a}} + 1\right)^{k_{3}}$$

where  $\theta$  is bulk stress,  $w_c$  is water content.

### **Integration of Matric Suction in Pavement ME**

• Sensitive models for determination of the Resilient Modulus (Proposed Enhancements to Pavement ME Design, 2019)

Model Type	Model Formulation (detailed definitions of parameters in Appendix B)	Material Type
Moisture-sensitive Model	$\log \frac{M_R}{M_{Ropt}} = a + \frac{b - a}{1 + \exp\left[\ln \frac{-b}{a} + k_m \left(S - S_{opt}\right)\right]}$	Granular Base/ Subgrade Soil
Moisture-sensitive and Stress- dependent Model	$M_{R} = k_{2} + k_{3}(k_{1} - \sigma_{d}) + k_{s}(u_{a} - u_{w})$ $M_{R} = k_{2} + k_{4}(\sigma_{d} - k_{1}) + k_{s}(u_{a} - u_{w})$	Subgrade Soil
Moisture-sensitive and Stress- dependent Model	$M_{R} = k_{1} P a \left(\frac{I_{1} - 3k_{4}}{Pa}\right)^{k_{2}} \left(\frac{\tau_{oct}}{Pa}\right)^{k_{3}}$	Granular Base/ Subgrade Soil

#### **Integration of Matric Suction in Pavement ME**

 The Pavement ME suggests the Moisture - sensitive models for determination of the Resilient Modulus (Proposed Enhancements to Pavement ME Design, 2019) (cont.)

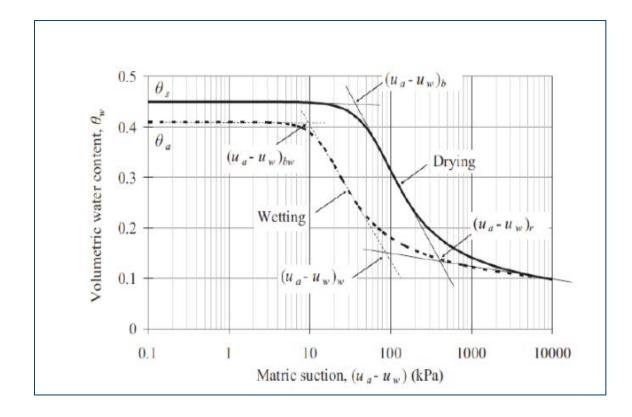
Model Type	Model Formulation (detailed definitions of parameters in Appendix B)	Material Type
Moisture-sensitive and Stress- dependent Model	$M_{R} = k_{1} P a \left(\frac{I_{1} - 3\theta f h_{m}}{Pa}\right)^{k_{2}} \left(\frac{\tau_{oct}}{Pa}\right)^{k_{3}}$	Granular Base/ Subgrade Soil
Moisture-sensitive and Stress- dependent Model	$M_{R} = k_{1}Pa \left[ \frac{I_{1} - 3\theta f \left( h_{m} + \beta \frac{I_{1}}{3} + \alpha \tau_{oct} \right)}{Pa} \right]^{k_{2}} \left( \frac{\tau_{oct}}{Pa} \right)^{k_{3}}$	Granular Base/ Subgrade Soil
Moisture-sensitive and Stress- dependent Model	$M_{R} = k_1 \left(\sigma_d + \chi_w \psi_m\right)^{k_2}$	Subgrade Soil

### **Integration of Matric Suction in Pavement ME**

• The Pavement ME suggests the Moisture - sensitive models for determination of the Resilient Modulus (Proposed Enhancements to Pavement ME Design, 2019) (cont.)

Model Type	Model Formulation (detailed definitions of parameters in Appendix B)	Material Type
Moisture-sensitive and Stress- dependent Model	$M_{R} = k_{1}P_{a}\left(\frac{\theta + \chi_{w}\psi_{m}}{P_{a}}\right)^{k_{2}}\left(\frac{\tau_{oct}}{P_{a}} + 1\right)^{k_{3}}$	Subgrade Soil
Moisture-sensitive and Stress- dependent Model	$M_{R} = k_{1}P_{a}\left(\frac{\theta_{net} - 3\Delta u_{w-sat}}{P_{a}}\right)^{k_{2}}\left(\frac{\tau_{oct}}{P_{a}} + 1\right)^{k_{4}}\left(\frac{\psi_{m_{o}} - \Delta\psi_{m}}{P_{a}} + 1\right)^{k_{4}}$	Granular Base
Moisture-sensitive and Stress- dependent Model	$M_{R} = k_{1} p_{a} \left(\frac{\sigma_{b} - 3k_{6}}{p_{a}}\right)^{k_{2}} \left(k_{7} + \frac{\tau_{oct}}{p_{a}}\right)^{k_{3}} + k_{us} p_{a} \Theta^{\kappa} \left(\mu_{a} - \mu_{w}\right)$	Subgrade Soil

**Freeze-Thaw Cycles** 



(Albadri et al., 2020)

### Effect of Freeze – Thaw Action in Resilient Modulus

- Three factors are introduced to account for base/subgrade resilient modulus due to freeze – thaw action
  - Reduction Factor (RF)
  - Recovery Ratio (RR)
  - Environmental Adjustment Factor (F<sub>env</sub>)

### Environmental Adjustment Factor (F<sub>env</sub>)

$$F_F = \frac{M_{Rfzr}}{M_{Ropt}}$$

$$F_R = RF + R_{equil} * RR - RR * RF \qquad \text{if } S_{equil} - S_{opt} < 0$$

$$F_R = R_{equil} * (RF + RR - RR * RF) \quad \text{if } S_{equil} - S_{opt} > 0$$

$$\log F_{U} = \log \frac{M_{R}}{M_{Ropt}} = a + \frac{b-a}{1 + EXP(\ln \frac{-b}{a} + k_{m}(S - S_{opt}))}$$

where,

 $M_R$ = Resilient modulus at unfrozen / normal condition  $M_{Ropt}$ = Resilient modulus at a reference condition  $M_{Rfzr}$ = Resilient modulus at a frozen condition

## Environmental Adjustment Factor (F<sub>env</sub>)

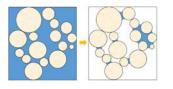
$$M_R = F_{env} * k_1 * p_a * \left(\frac{\theta}{p_a}\right)^{k_2} * \left(\frac{\tau_{oct}}{p_a} + 1\right)^{k_3}$$

#### where,

 $M_R$  = stress dependent resilient modulus  $F_{env}$  = composite environmental adjustment factor  $k_1, k_2, k_3$  = regression coefficients  $p_a$  = atmospheric pressure  $\theta$  = bulk stress

 $\tau_{oct}$  = octahedral shear stress

THANK YOU



### Correlations between Unsaturated Soil Parameters and Pavement-ME Design Input

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#### NRRA Webinar May 19, 2020









## **Relationship between Matric Suction and Stiffness Properties of Materials**

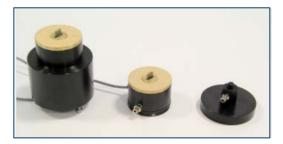
Maximum Shear Modulus – G<sub>max</sub> (G<sub>o</sub>):

Measurement of Shear Wave Velocity



$$G = \rho \times v_s^2$$

where  $\rho$  is density and  $\mathcal{V}_{S}$  is shear wave velocity.



**Bender Element** 



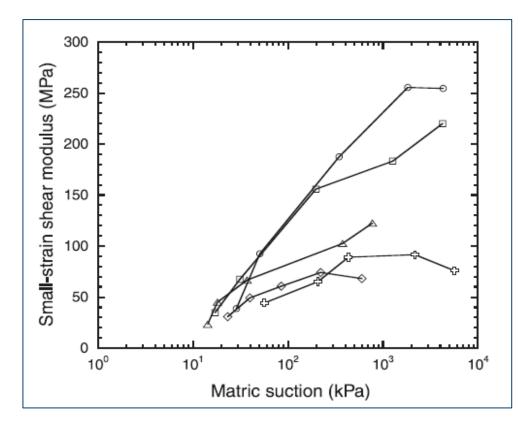
**Ultrasonic Velocity Test** 



Resonant Column

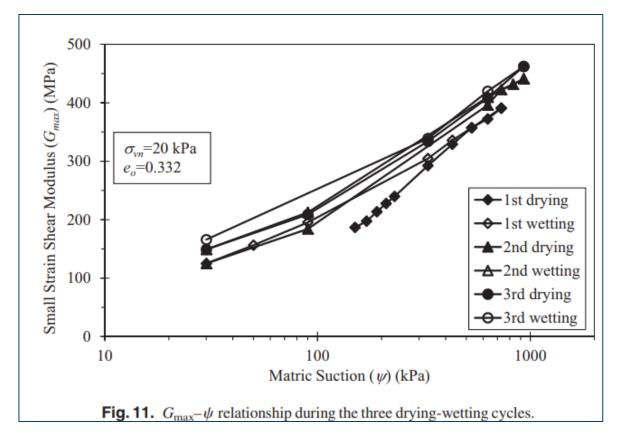
## Relationship between Matric Suction and Stiffness Properties of Materials

- Four key factors that directly influence the magnitude of G<sub>max</sub>
- Void ratio
- Net stress
- Matric Suction
- Saturation degree



#### (Sawangsuriya et al. 2008)

• Effect of wetting and drying cycles on Maximum shear modulus



(Ngoc et al., 2019)

Correlations between Maximum Shear Modulus and Matric Suction

$$G_{max} = p_r f(e) \left[ b_1 \left( \frac{\psi S_r}{p_r} \right)^{m_1} + c(1 - S_r)^k \right] \text{ for } S_r \ge S_{rs}$$

$$G_{max} = p_r f(e) \left[ b_2 \left( \frac{\psi S_r}{p_r} \right)^{m_2} + c(1 - S_r)^k \right] \text{ for } S_r < S_{rs}$$

$$\frac{G_o}{w\xi \omega} = \alpha \log \psi - \beta$$

$$G_o = \left( w \frac{E}{E_{std}} \frac{w_{opt}}{w_{opt,std}} \right) (\alpha \log \psi - \beta)$$
Sawangsuriya et al., 2008

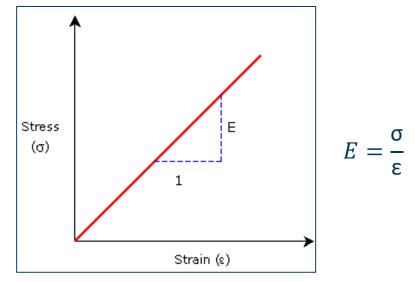
# Relationship between Matric Suction and Stiffness

**Properties of Materials** 

## • Young's Modulus - E

Uniaxial test  $\blacksquare$  Stress( $\sigma$ ) – strain relationship( $\epsilon$ )  $\blacksquare$ 

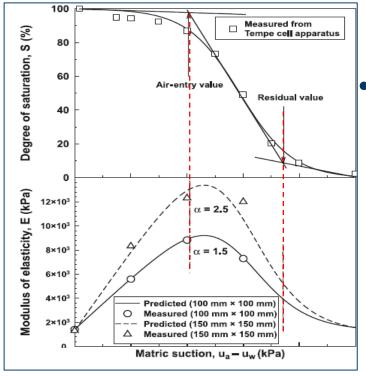
#### Young's Modulus





#### **Triaxial Testing**

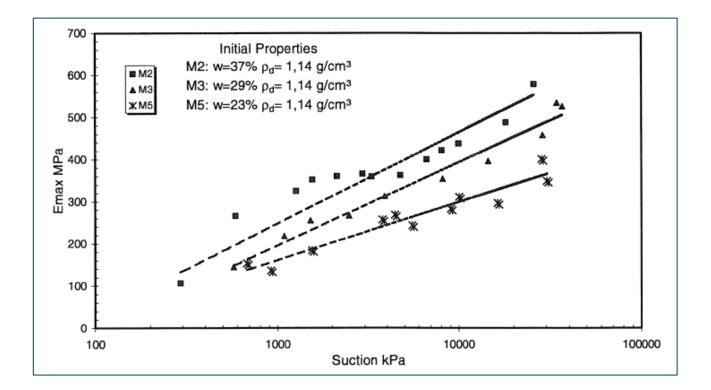
• Relationship between Young's Modulus and Matric Suction



(Oh et al., 2009)

- Moduli of elasticity behavior is different in the three stages of desaturation: the boundary effect zone, transition zone, and residual zone (Vanapalli et al. 1999).
  - Boundary effect zone
  - Transition zone
  - Residual zone

Relationship between Young's Modulus and Matric Suction



(Mendoza and Colmenares 2006)

Correlations between Modulus of Elasticity and Matric Suction

$$E_{\text{unsat}} = E_{\text{sat}} + E_{\text{sat}} \alpha \frac{(u_{\text{a}} - u_{\text{w}})}{(P_{\text{a}}/100)} (S^{\beta})$$

(Oh et al. 2009)

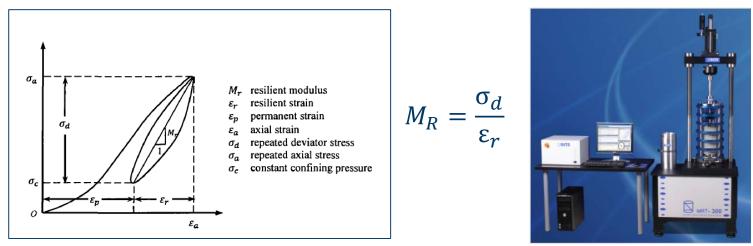
$$E_{max(unsat)} = 30000 \frac{(2.3 - e)^2}{1 + e} \left[ \ln(u_a - u_w) \right]^{1.35}$$

(Mendoza et al. 2005)

#### **Relationship between Matric Suction and Stiffness**

**Properties of Materials** 

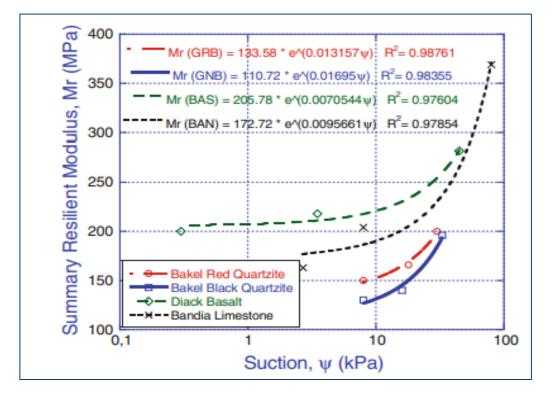
### Resilient Modulus - M<sub>R</sub>



Resilient Modulus Testing Systems

#### (Yingliu 2010)

• Relationship between Resilient Modulus and Matric Suction

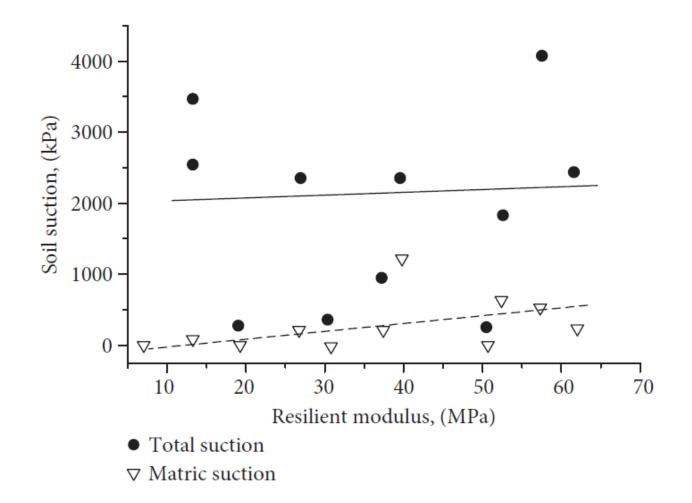


(Ba et al. 2013)

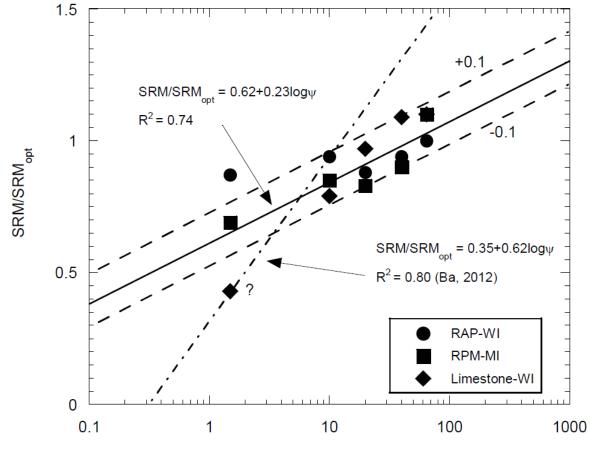
#### **Materials**

Correlations between Resilient Modulus and Matric Suction

 $M_R/M_{ROPT} = 0.385 + 0.267 \log (\psi)$ Ba et al., 2013  $M_R = 142 + 16.9\psi$ Ceratti et al., 2004  $M_R = k_1 p_a \left(\frac{\theta_b}{p_a}\right)^{k_2} \left(k_4 + \frac{\tau_{oct}}{p_a}\right)^{k_3} + \alpha_1 \psi^{\beta_1}$ Khoury et al., 2009  $M_R = k_1 p_a \left(\frac{\theta_b - 3f\theta \psi}{p_a}\right)^{k_2} \left(\frac{\tau_{oct}}{p_a}\right)^{k_3}$ Lytton, 1995

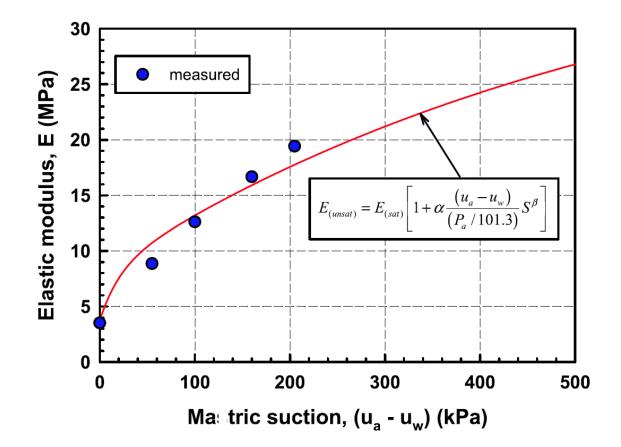


(Chu 2020)



Matric Suction (kPa)

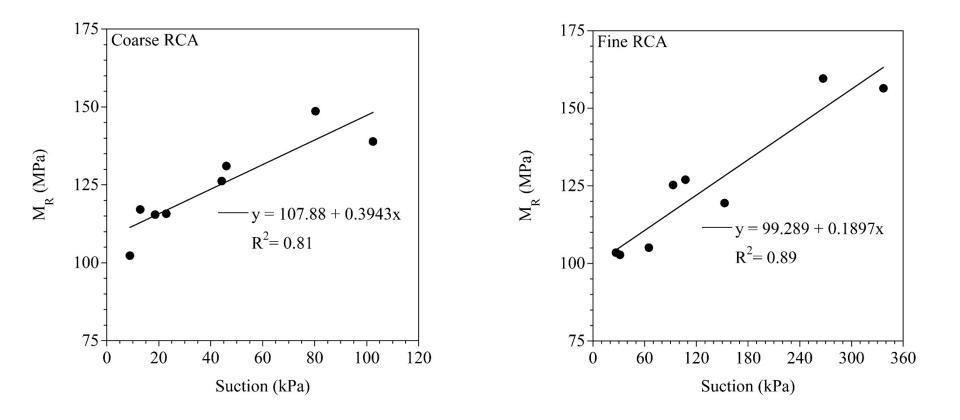
(Nokkaew et al. 2013)

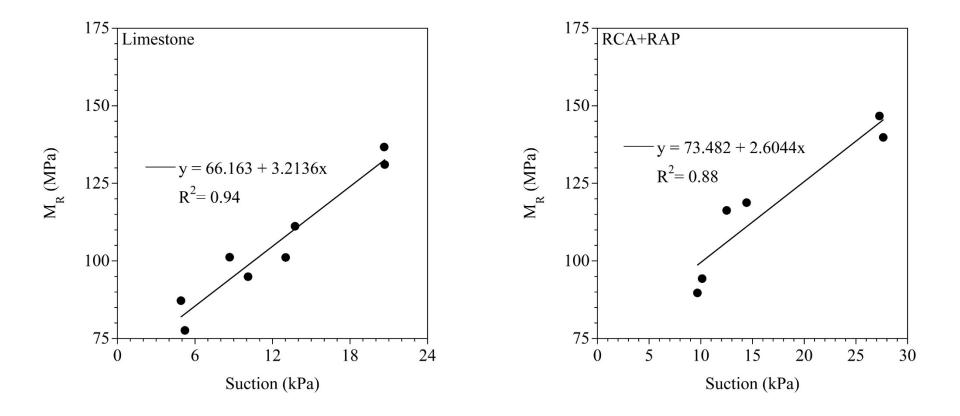


(Oh and Vanapalli 2018)

## **NRRA Funded Project Results**

Recycled Aggregate Base				Large Stone Subbase		Large Stone Subbase with Geosynthetics					
185	186	188	189	127	227	328	428	528	628	728	
3.5 in Superpave	3.5 in Superpave	3.5 in Superpave	3.5 in Superpave	3.5 in Superpave	3.5 in Superpave	3.5 in Superpave	3.5 in Superpave	3.5 in Superpave	3.5 in Superpave	3.5 in Superpave	
12 in Coarse RCA	12 in Fine RCA	12 in Limestone	12 in RCA+RAP	6 in Class 6 Aggregate	6 in Class 6 Aggregate	6 in Class 5Q Aggregate	6 in Class 5Q Aggregate	6 in Class 5Q Aggregate	6 in Class 5Q Aggregate	6 in Class 5Q Aggregate	
				18 in LSSB (1 lift)	18 in LSSB (1 lift)	9 in LSSB TX	9 in LSSB TX+GT	9 in LSSB BX+GT	9 in LSSB BX	9 in LSSB	
3.5 in S. Granular Borrow	3.5 in S. Granular Borrow	3.5 in S. Granular Borrow	3.5 in S. Granular Borrow								
Sand	Sand	Clay Loam	Clay Loam			Clay Loam	Clay Loam	Clay Loam	Clay Loam	Clay Loam	
S. Granular Borrow = Select Granular Borrow						TX = Triaxial Geogrid BX = Biaxial Geogrid					
				Clay Loam	Clay Loam	GT = Nonwoven Geotextile					





## SUMMARY

- Determination of the Resilient Modulus for various matric suctions / water contents / saturation degree has a significant effect on the design process of long - lasting pavement structures.
  - The effect of various climate and traffic conditions
  - The moisture-sensitive models

#### Improved Prediction of the Pavement Response

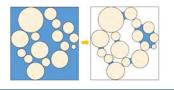




## **SUMMARY**

- In various engineering designs such as compacted subgrades and support fills for highways, railroads, airfields, parking lots, earthquake resistant structures and foundations the Soil Modulus is required.
- Soil Modulus (G<sub>max</sub>, E, M<sub>R</sub>) which represents the stiffness of geomaterials for different cases is related to Matric Suction.

<u>Knowing the Effect of Matric Suction will Increase the Accuracy of the Design of</u> <u>Engineering Structures!</u>



## Unsaturated Soil Mechanics at MnDOT

### John Siekmeier P.E.

#### NRRA Webinar May 19, 2020









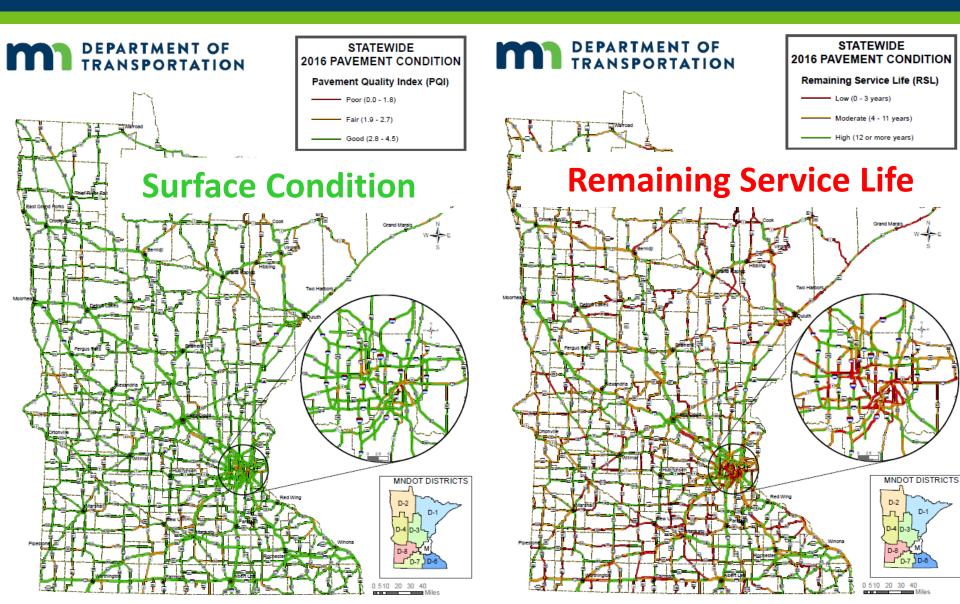
## Acknowledgements

- Counties, Cities and MnDOT Districts
- Federal Highway Administration and State DOTs
- Manufacturers, Contractors and Consultants
- Universities and the National Academies

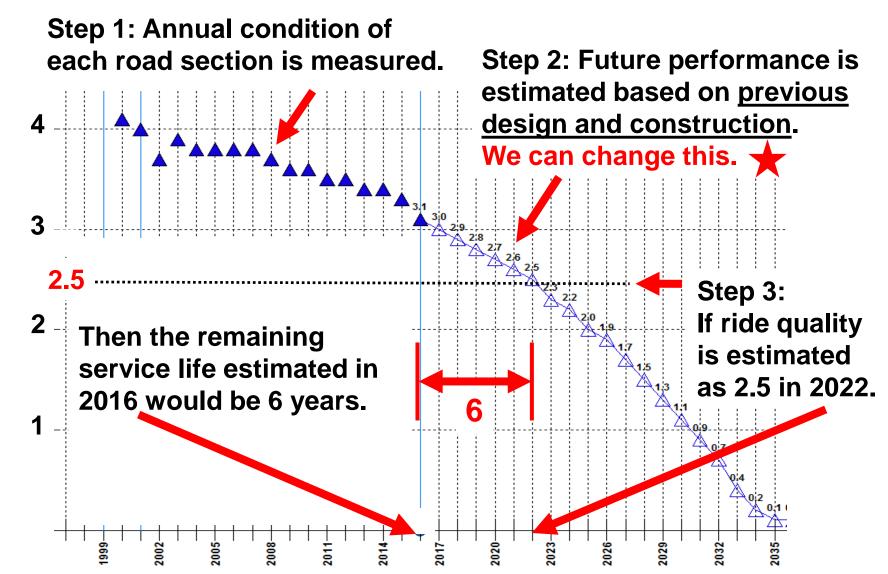
## Outline

- Pavement Foundations are Important
- Pavement Design Framework
- Performance Based Specifications
- Lessons Learned

## **Pavement Foundations are Important**

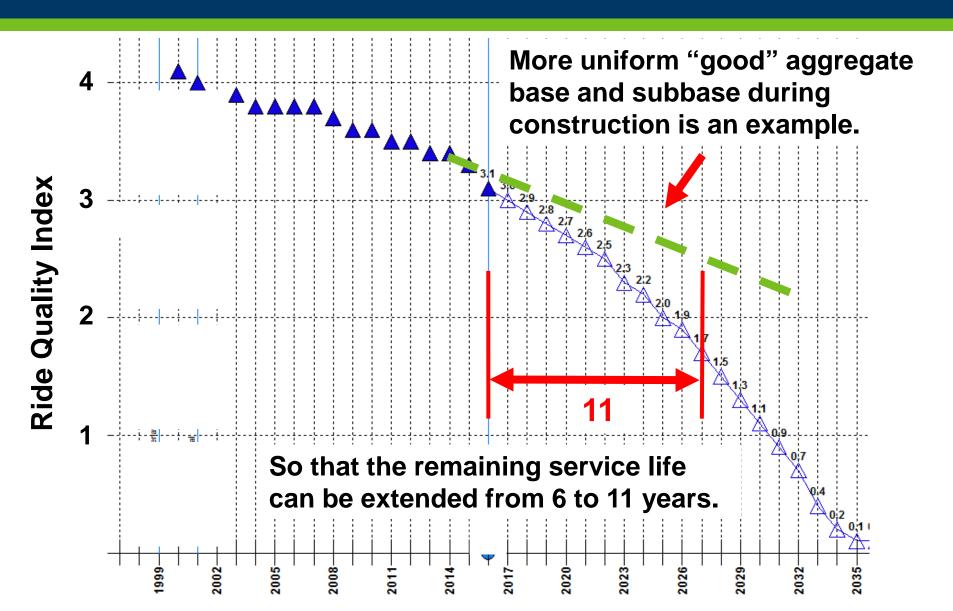


## What is Remaining Service Life?

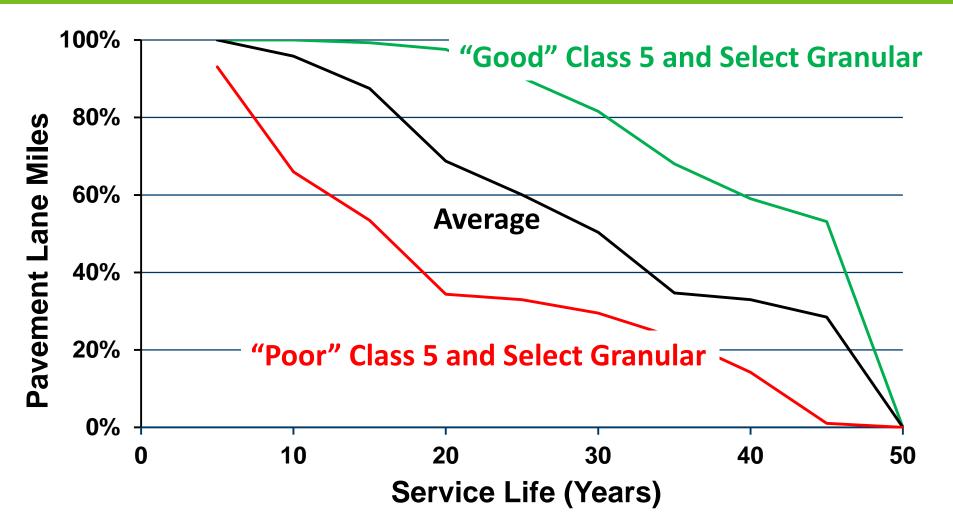


# Ride Quality Index

## Need to Construct Better Foundations



## Importance of Good Base and Subbase



Courtesy of Erol Tutumluer, Best Value Granular Project, July 20, 2010

## Cost Effective Pavement Design 2002

March 20, 2002

DATE:

TO:

District Engineers (DISTENG), District Materials Engineers, District State Aid Engineers (DSAE) VIA Groupwise

FROM: Gerald J. Rohrbach, Director Office of Materials & Road Research

A seals J. Robernach

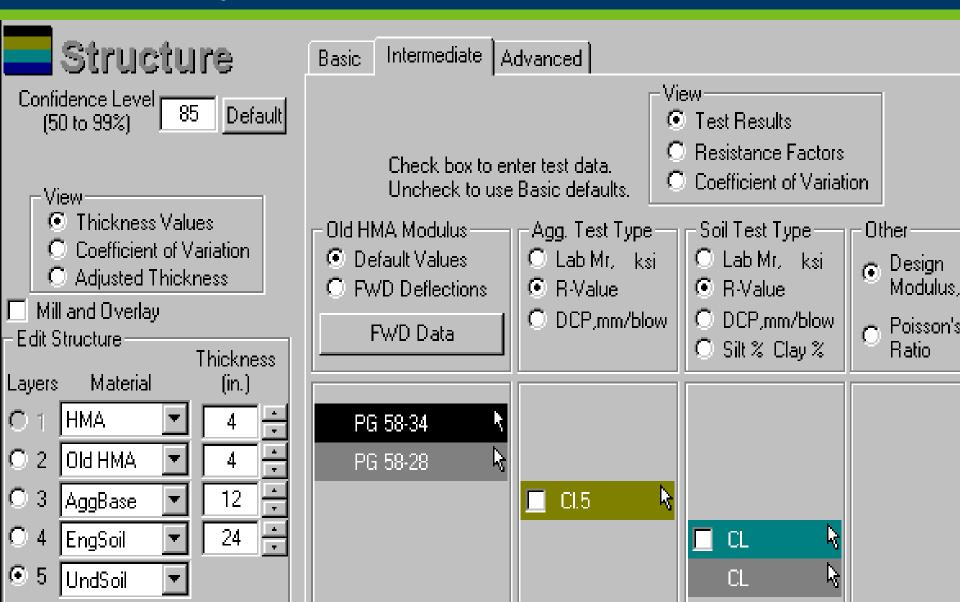
**PHONE:** 65,1-779-5590

SUBJECT: Mn/PAVE – Mechanistic-Empirical Thickness Design Procedure for Flexible Pavements.

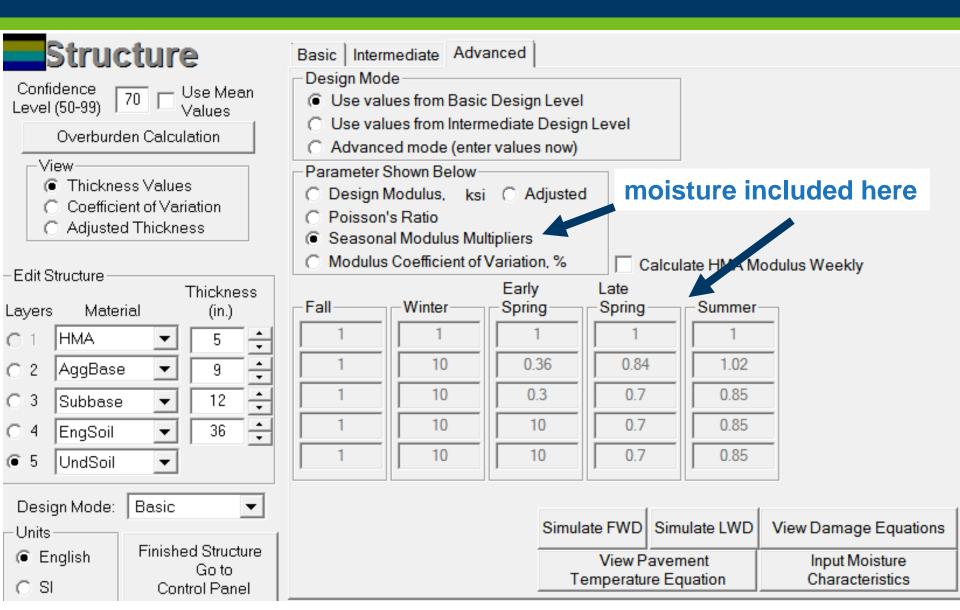
Through cooperative efforts with the University of Minnesota and the Local Road Research Board, the Minnesota Department of Transportation has developed a software program entitled MnPAVE. MnPAVE is a mechanistic-empirical design procedure based on structural analysis of a layered pavement system and is intended for use by state and local agencies. It is now time to move into the training/implementation phase and begin using the design procedure on a trial basis.

MnPAVE has several key advantages over our current Mn/DOT design procedures. These include the capability to 1) adapt to different distress modes, 2) implement better materials tests, 3) adapt to changing load limits and configurations, and 4) achieve agreement between structural and material design. In short, MnPAVE will allow agencies to design and construct more cost-effective flexible pavements.

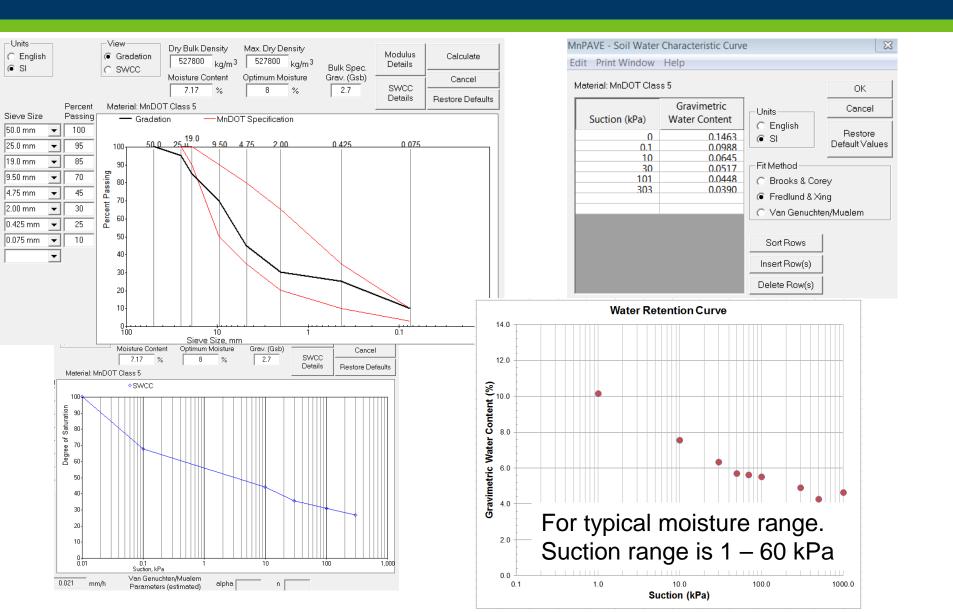
## MnPAVE Design Inputs are Layer Thickness and Stiffness



## MnPAVE also Requires Moisture Inputs



## Gradation used to Estimate Suction



## **Moisture Condition Case Studies**

Jill Ovik Thesis, 1998 seasonal properties

Ruth Roberson Thesis, 2007 unsaturated geomechanics

## Lessons Learned from Case Studies

- Modulus and strength are greatly affected by the moisture between the particles, which causes a suction or tensile stress between the particles.
- Tensile stress between particles depends on:
  - Gradation (quantity of sand, silt, and clay)
  - Particle shape (roughness)
  - Porosity (void space "openness")
  - Moisture content (how much water is in the voids)

## Construction request. Need to eliminate unsafe Testing



## MnPAVE Outputs are Pavement Life and Moisture Corrected LWD Deflections



Surface	Field	Field	LWD Deflection (mm) at top of Surface Material								
Material	Modulus	Resistance									
	(MPa)	Factor	Opt20%	Opt10%	Optimum	Opt.+10%	Opt.+20%				
			Estimated Target Values								
AggBase	180.5	1.15	0.52	0.55	0.60	0.66	0.71				
EngSoil	29.98	0.96				Х					
UndSoil	19.23	0.75			X						

Simulated using material properties from Intermediate design level.

## **Performance Based Specifications**

## Ralph Proctor reminds us.

- Density does not determine strength.
- Optimum moisture is for compaction.
- Need to avoid rutting during construction.

Photo courtesy of Dr. J. David Rogers Missouri University Science & Technology



## Bouquet Canyon Dam 1932-34

Photo courtesy of Dr. J. David Rogers Missouri University Science & Technology

## Ralph Proctor, 1945, Trans 110, ASCE

- "No use is made of the actual peak dry weight."
- "Methods for hand compaction, such as dropping various weight tampers from different heights and mechanical tampers, were tried and discarded."
- "The measure of soil compaction used is the indicated saturation penetration resistance."

## **Proctor Penetrometer Performance Test**

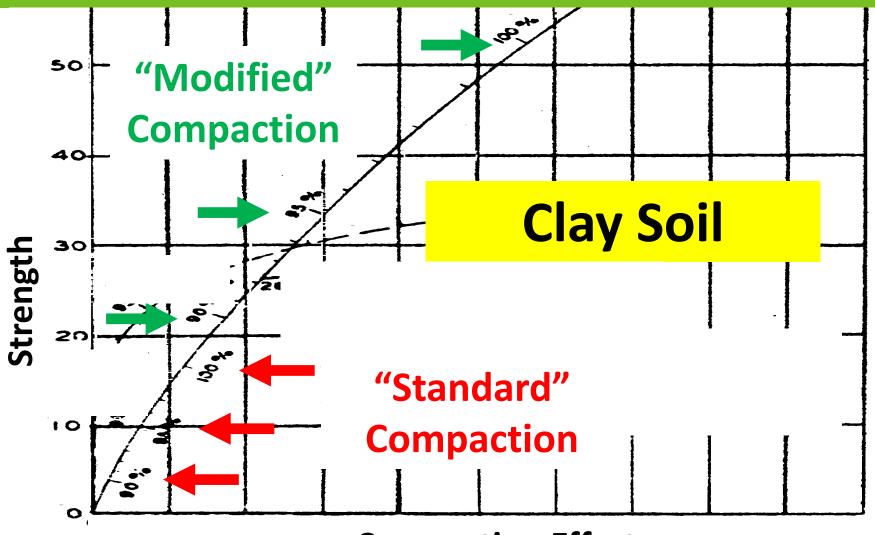


Photo courtesy of Humboldt

# What went wrong during WWII ? Density was used, not penetration test.

Photo courtesy of Dr. J. David Rogers Missouri University Science & Technology

## Strength Compared to Density, Proctor 1948

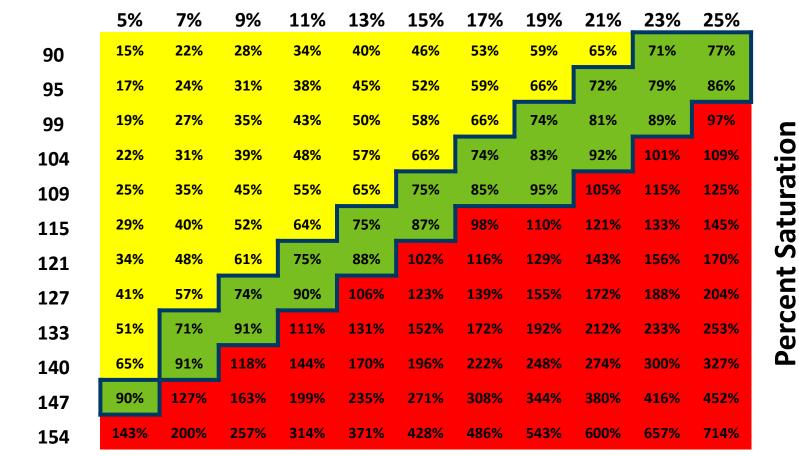


**Compaction Effort** 

## **Density Does Not Determine Strength**



# **Need Correct Moisture for Compaction**



**Moisture Content** 

Courtesy of Soheil Nazarian, 2018 NRRA Pavement Workshop, May 23-24, 2018

## **Construction Tests Verify Design Properties**



### Dynamic Cone Penetrometer

### ASTM D 6951-03

### Grading and Base Manual, MnDOT



# Light Weight Deflectometer

### ASTM E 2583 07 (includes load measurement)

### ASTM E 2835 11 (no load measurement)

### Grading and Base Manual, MnDOT



# DCP and LWD Aggregate Base Target Values

Grading Number	Moisture Content	Dynamic Cone Penetrometer Target Value	Light Weight Deflectometer Target Value
	%	mm / drop	mm
3.1-3.5	5 - 7	10	0.38
	7 - 9	12	0.45
	9 - 11	16	0.60
3.6-4.0	5 - 7	10	0.38
	7 - 9	15	0.56
	9 - 11	19	0.71
4.1-4.5	5 - 7	13	0.49
	7 - 9	17	0.64
	9 - 11	21	0.79

## Minnesota LWD Specification

#### S-47.3 CONSTRUCTION REQUIREMENTS

Compact the entire lift to achieve the LWD-TV per Table 1. Either LWD-TV parameter (Maximum Allowable Deflection or Minimum Allowable Elastic Modulus) may be used, unless specifically designated in the contract. Ensure the same LWD-TV parameter is used throughout the entire project. Re-evaluate the selected LWD-TV, and contact the Grading and Base Engineer, when failing results consistently occur and adequate compaction is observed through quality compaction.

Table 1: LWD Target Values						
Specification	Material Type	Maximum Allowable	Minimum Allowable			
		Deflection (mm)	Elastic Modulus (MPa)			
2105 or 2106	Granular	0.78	40			
	Clay and Clay Loam	1.47	20			
2211	Base	0.55	50			

### **MnDOT Detroit Lakes**

### Indiana LWD Specification

Material Type	Average	Maximum at a Single Location
Lime Modified Soil	≤ 0.30	0.35
Cement Modified Soil	≤ 0.27	0.31
Aggregate over Lime Modified Soil	≤ 0.30	0.35
Aggregate over Cement Modified Soil	≤ 0.27	0.31

#### Table 2. Aggregate over Untreated Soils Where Proofrolling Can Be Performed

Material Type	Average	Maximum at a Single Location
6 in. Thick Coarse Aggregate No. 53	≤ 0.51	0.57
12 in. Thick Coarse Aggregate No. 53	≤ 0.34	0.40
18 in. Thick Coarse Aggregate No. 53	≤ 0.31	0.35

#### Table 3. Aggregate over Untreated Soils Where Proofrolling Cannot Be Performed

Material Type	Average	Maximum at a Single Location
6 in. Thick Coarse Aggregate No. 53	≤ 0.60	0.65
12 in. Thick Coarse Aggregate No. 53	≤ 0.47	0.52
18 in. Thick Coarse Aggregate No. 53	≤ 0.44	0.49

# **AASHTO Draft Specifications**

- Just Google "NRRA Geotechnical Team"
- Standard Specification for Quality Management of Earthwork and Pavement Foundation Layers using Modulus
- Acknowledgements
  - Maryland DOT Transportation Pooled Fund 5-285
  - University Texas El Paso NCHRP 10-84
    - NCHRP 24-45 new April 2020

## Lessons Learned and Next Steps

- DCPs and LWDs can be used during construction to verify design values.
- It is important to measure moisture because both our ability to compact soils and aggregates, and their long term performance requires knowledge of the moisture content.
- Implementation continues so that the people's investments are well spent.

# Thanks for Listening. Please ask questions.

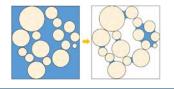
It's not rocket science. It is rock science.

### john.Siekmeier@state.mn.us

a. 1. 6

### **Moisture Tension in Sand**

### https://www.youtube.com/watch?v=a-6YbkZJ5UY



### Q&A – Applications

### All

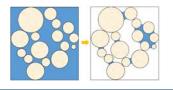
### NRRA Webinar May 19, 2020











### **Closing Remarks**

### Terry Beaudry P.E.

### NRRA Webinar May 19, 2020









### THANK YOU!





Department of Civil and Environmental Engineering UNIVERSITY OF WISCONSIN-MADISON

